

# Experiment-Driven Characterization of Full-Duplex Wireless Systems

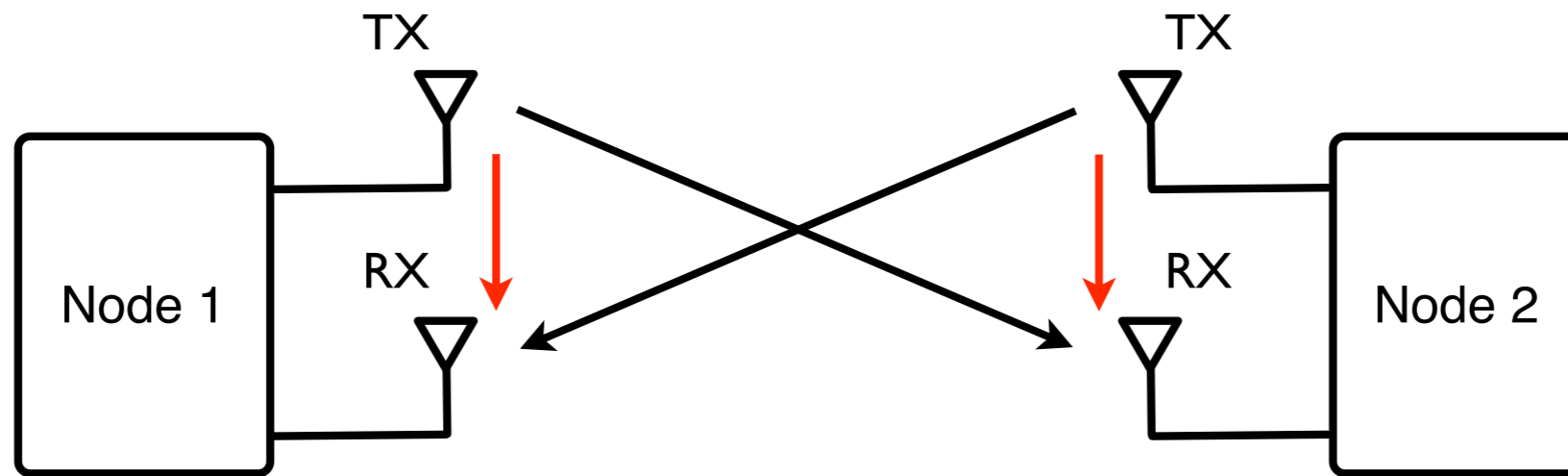
Melissa Duarte

Advisor: Ashutosh Sabhawal

Department of ECE  
Rice University

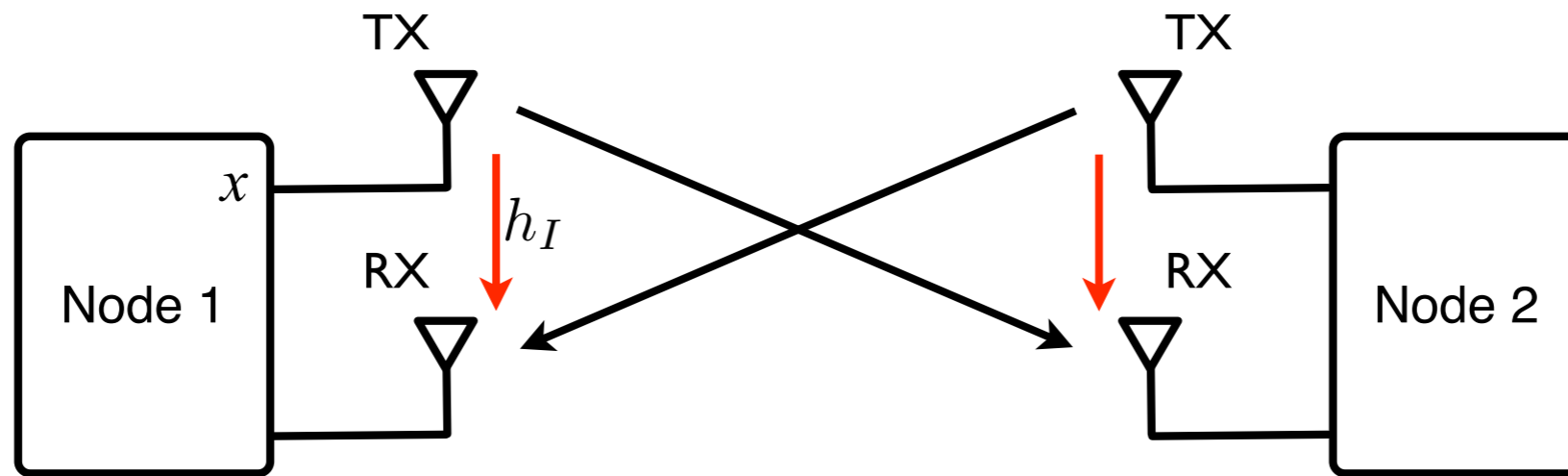
August 04 2011

# Full-Duplex Wireless



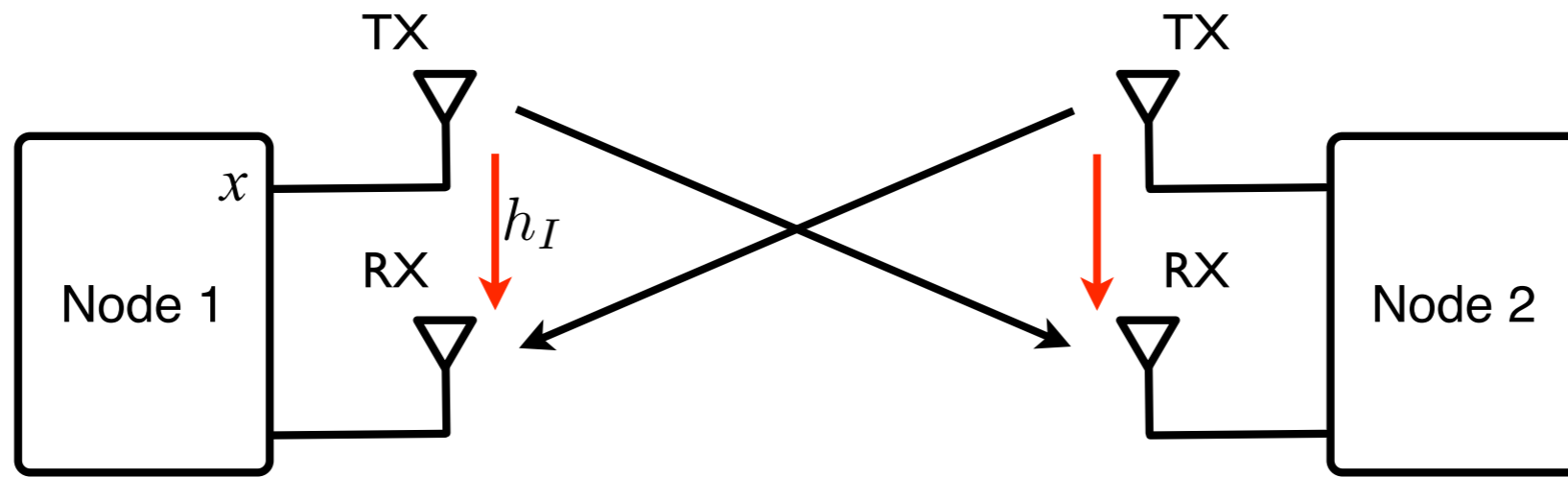
- Same time same frequency band
- Assumed to be impossible due to large self interference
- Revisit this assumption using techniques for interference cancellation
- Can full-duplex achieve higher data rates than half-duplex ?
- Characterize amount of cancellation and achievable rate performance

# Interference Problem



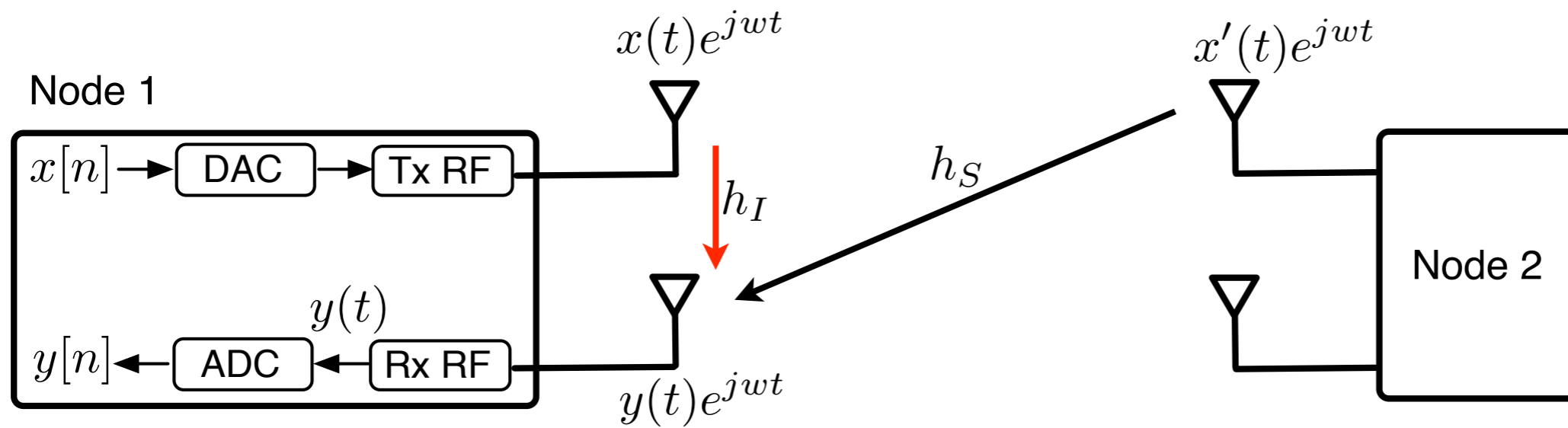
- Theory
  - Interference  $\gg$  Signal
  - Strong interference regime
  - Interference is known, estimate channel, cancel, done

# Interference Problem



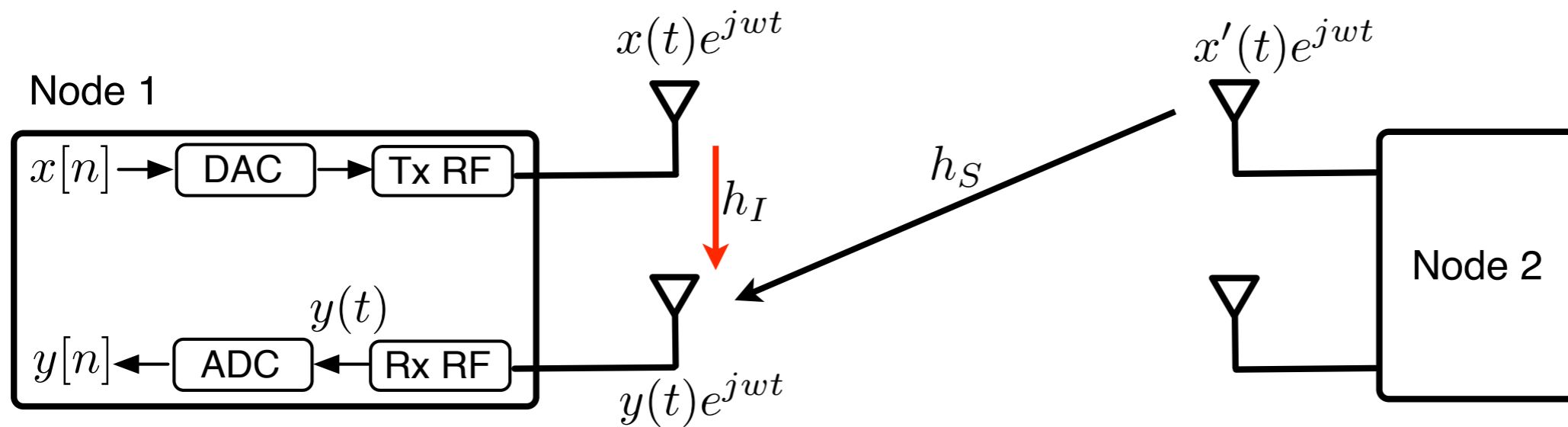
- Implementation

# Interference Problem



- Implementation

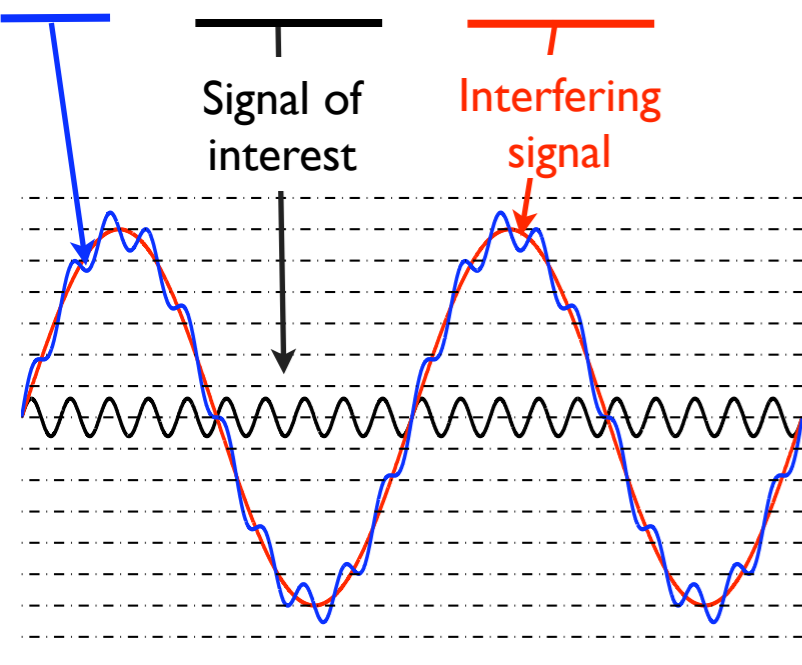
# Interference Problem



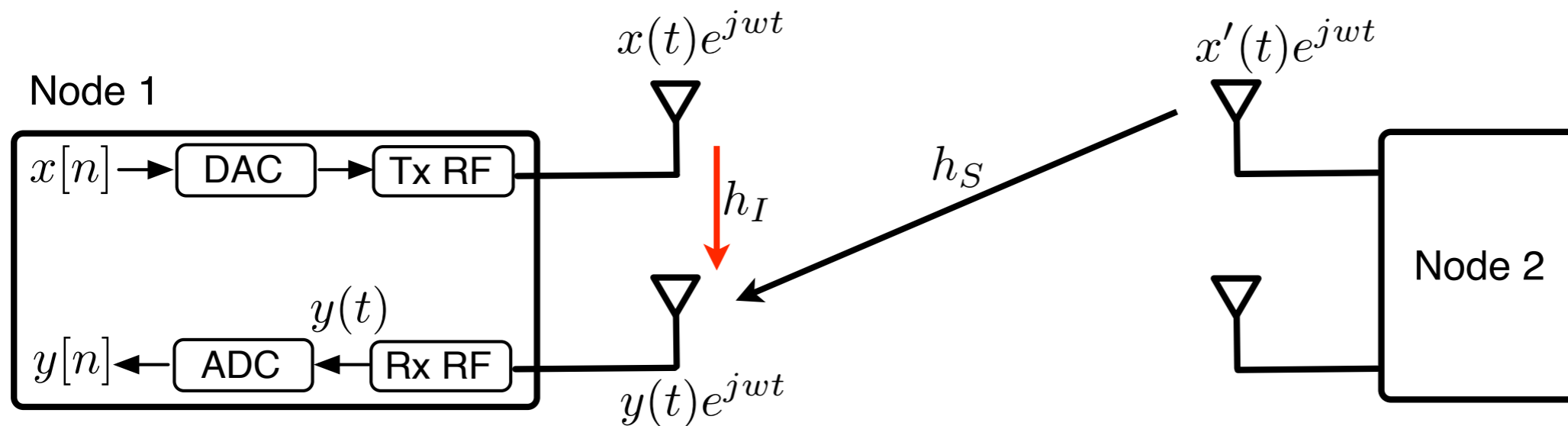
- Implementation

- Received signal

$$y(t) = h_S x'(t) + h_I x(t) + z(t)$$



# Interference Problem



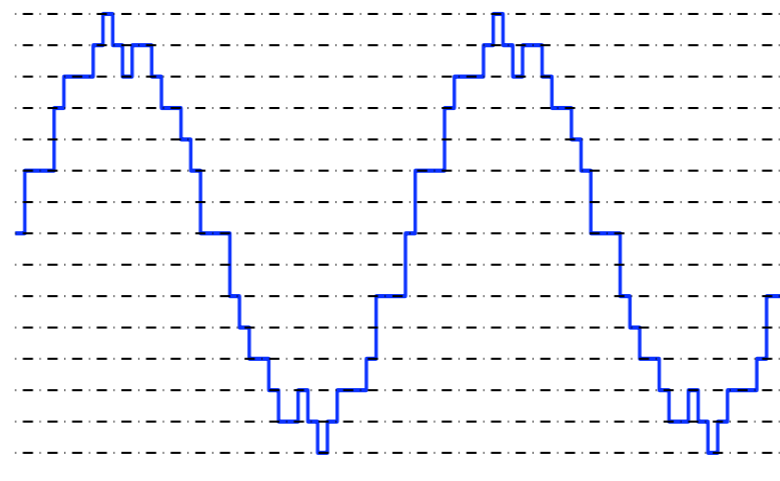
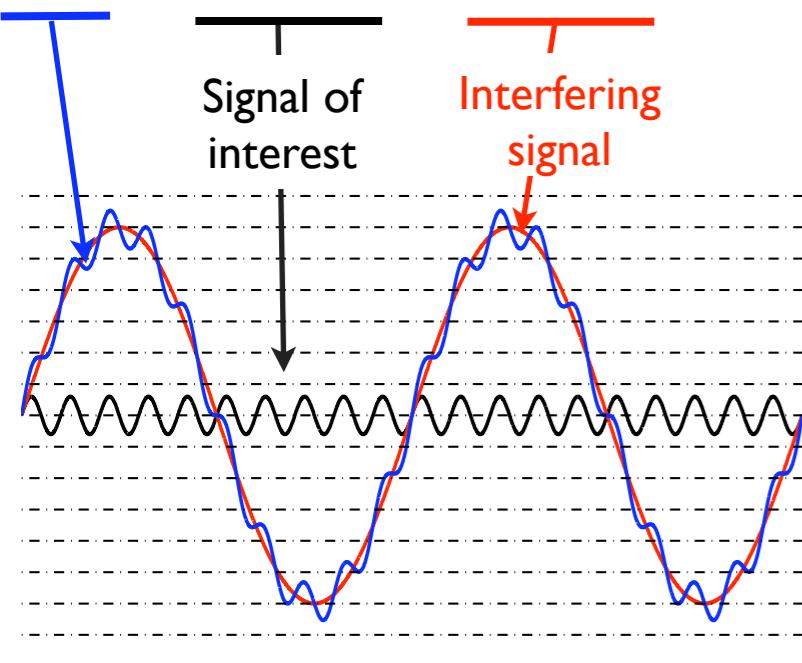
- Implementation

- Received signal

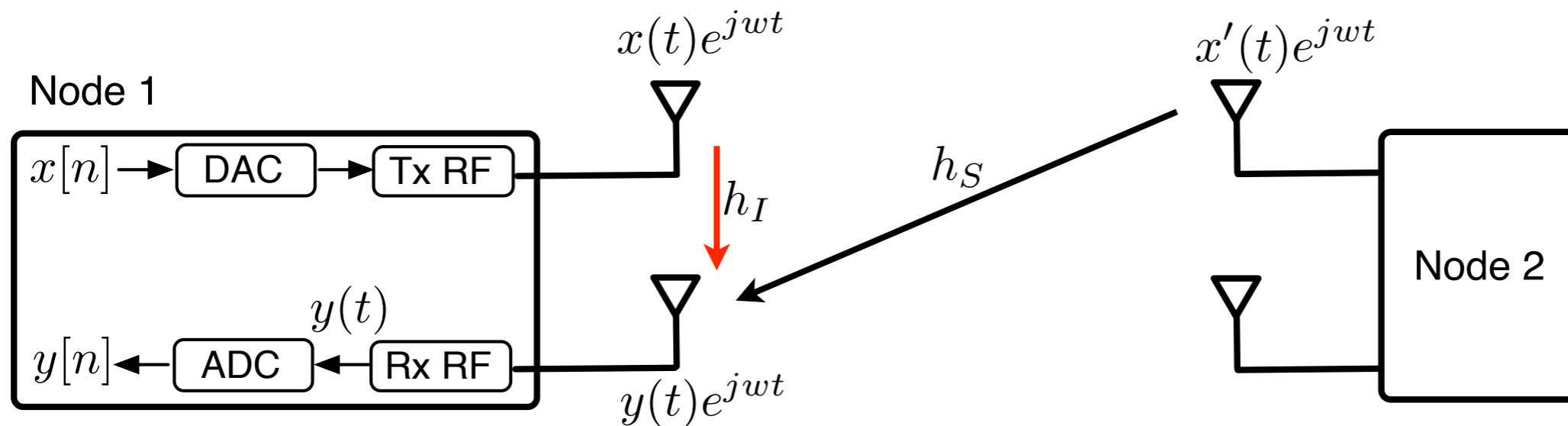
- Quantized received signal

$$y(t) = h_S x'(t) + h_I x(t) + z(t)$$

$$y[n] = h_S x'[n] + h_I x[n] + z[n]$$



# Interference Problem



- Implementation

- Received signal

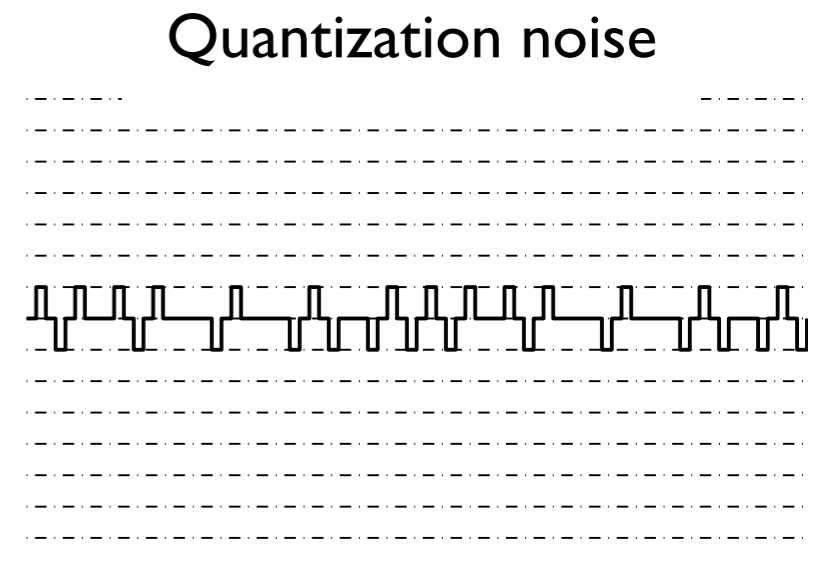
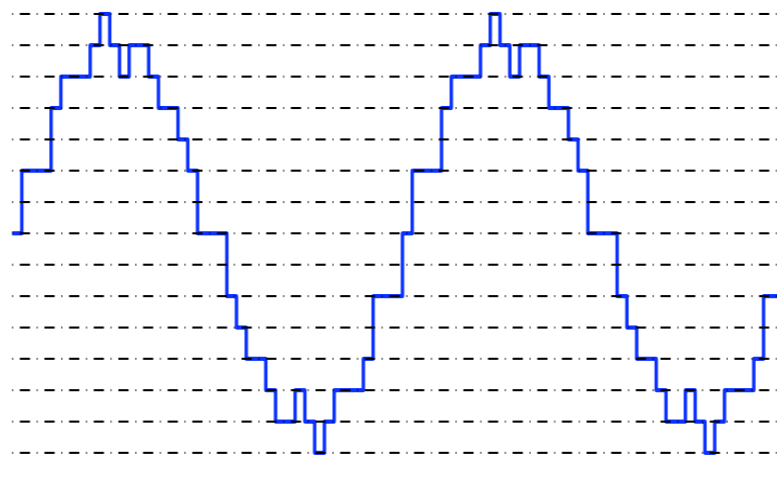
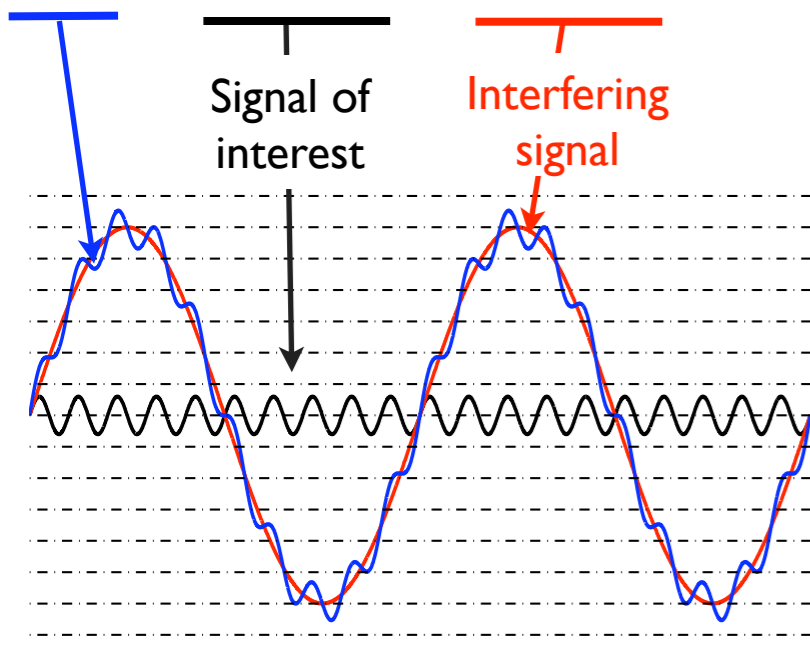
- Quantized received signal

- After removing interference

$$y(t) = h_S x'(t) + h_I x(t) + z(t)$$

$$y[n] = h_S x'[n] + h_I x[n] + z[n]$$

$$y[n] = h_S x'[n] + z[n]$$

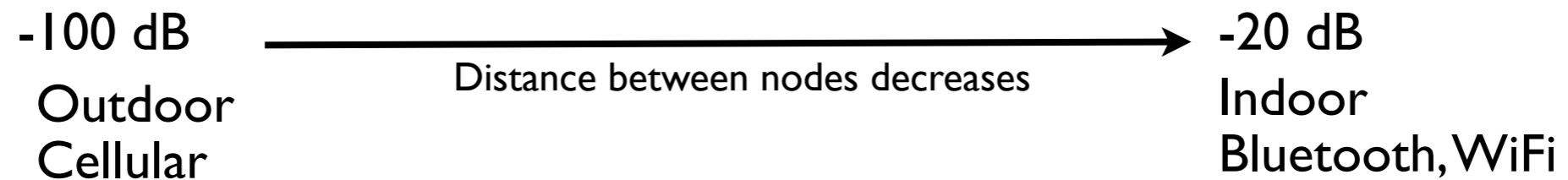




# Interference Problem

- Implementation
  - Interference  $\gg$  Signal : Quantization noise
  - Full-duplex assumed to be impossible due to large self interference

- Real systems SIR



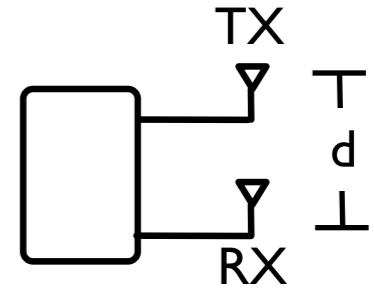
- More than 20 dB cancellation has been reported in radar systems
- Revisit this assumption using **passive** and **active** techniques for interference cancellation

# Passive Cancellation

- Antenna Separation
- Antenna Directionality
- Antenna Cancellation
- Device Cancellation

# Passive Cancellation

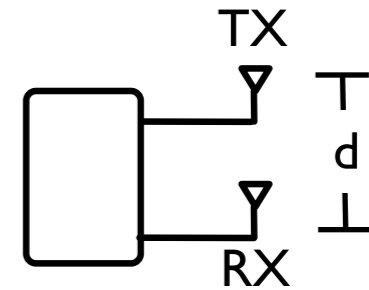
- Antenna Separation  
Separation  $d$  between same node Tx and Rx antennas
- Antenna Directionality
- Antenna Cancellation
- Device Cancellation



# Passive Cancellation

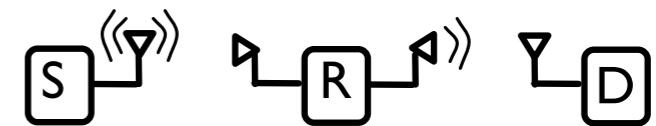
- Antenna Separation

Separation  $d$  between same node Tx and Rx antennas



- Antenna Directionality

Used in Full-duplex Relays



Everett et. al. *Empowering Full-Duplex Wireless Communication by Exploiting Directional Diversity*. Asilomar 2011.

Haneda et. al. *Measurement of Loop-Back Interference Channels for Outdoor-to-Indoor Full-Duplex Radio Relays*. Eucap 2010.

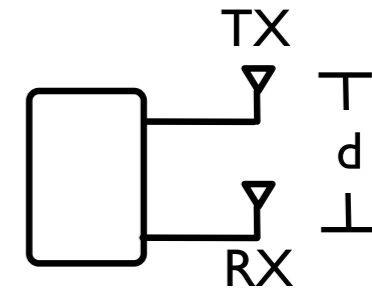
- Antenna Cancellation

- Device Cancellation

# Passive Cancellation

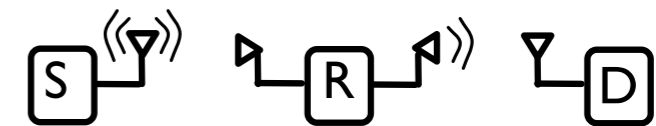
- Antenna Separation

Separation  $d$  between same node Tx and Rx antennas



- Antenna Directionality

Used in Full-duplex Relays



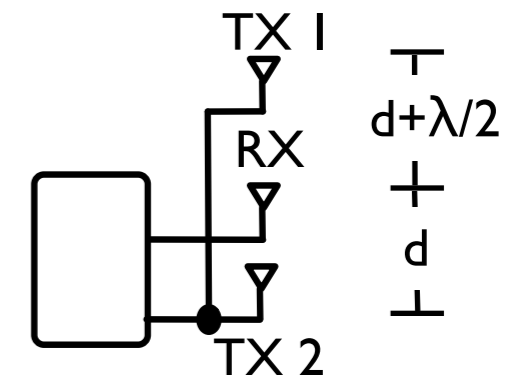
Everett et. al. *Empowering Full-Duplex Wireless Communication by Exploiting Directional Diversity*. Asilomar 2011.

Haneda et. al. *Measurement of Loop-Back Interference Channels for Outdoor-to-Indoor Full-Duplex Radio Relays*. Eucap 2010.

- Antenna Cancellation

2 Tx and 1 Rx per node, Tx at  $d$  and  $d+\lambda/2$

Choi et al. *Achieving Single Channel, Full Duplex Wireless Communication*. Mobicom 2010.

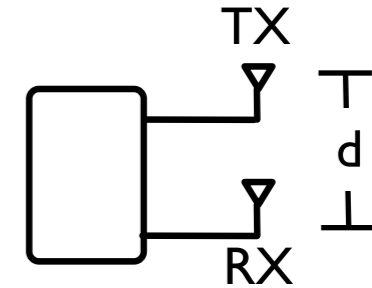


- Device Cancellation

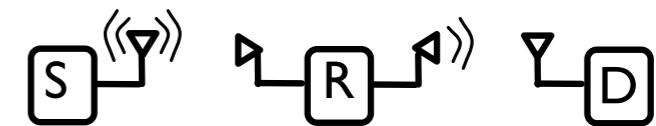
# Passive Cancellation

- Antenna Separation

Separation  $d$  between same node Tx and Rx antennas



- Antenna Directionality  
Used in Full-duplex Relays



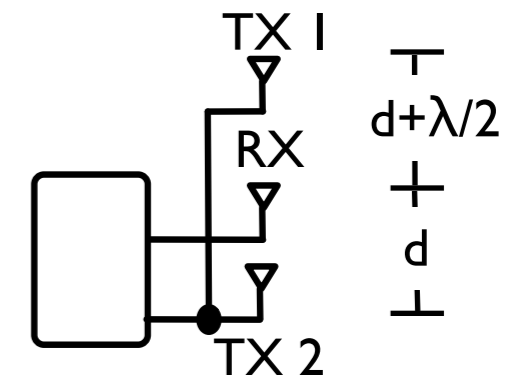
Everett et. al. *Empowering Full-Duplex Wireless Communication by Exploiting Directional Diversity*. Asilomar 2011.

Haneda et. al. *Measurement of Loop-Back Interference Channels for Outdoor-to-Indoor Full-Duplex Radio Relays*. Eucap 2010.

- Antenna Cancellation

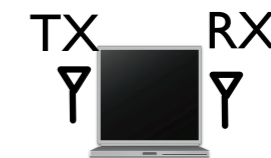
2 Tx and 1 Rx per node, Tx at  $d$  and  $d+\lambda/2$

Choi et al. *Achieving Single Channel, Full Duplex Wireless Communication*. Mobicom 2010.



- Device Cancellation

Place antennas at opposite sides of the device



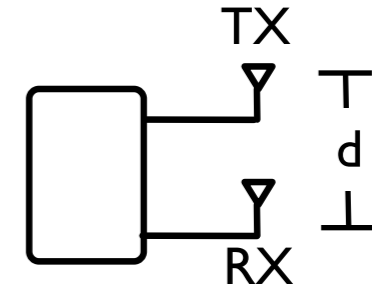
Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.

# Passive Cancellation

- Antenna Separation

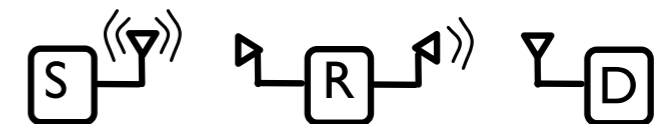
Separation  $d$  between same node Tx and Rx antennas

- We use antenna separation with  $d = 10\text{cm}, 20\text{cm}, 40\text{cm}$
- Worse case interference
- Minimum resources for passive cancellation



- Antenna Directionality

Used in Full-duplex Relays



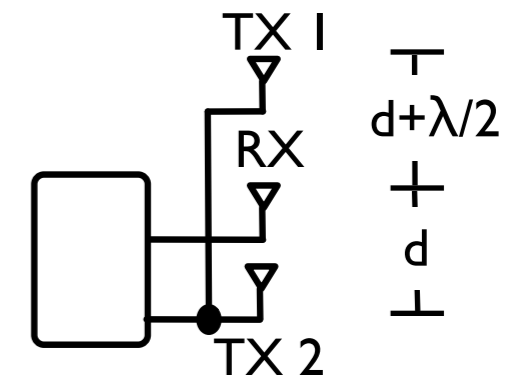
Everett et. al. *Empowering Full-Duplex Wireless Communication by Exploiting Directional Diversity*. Asilomar 2011.

Haneda et. al. *Measurement of Loop-Back Interference Channels for Outdoor-to-Indoor Full-Duplex Radio Relays*. Eucap 2010.

- Antenna Cancellation

2 Tx and 1 Rx per node, Tx at  $d$  and  $d + \lambda/2$

Choi et al. *Achieving Single Channel, Full Duplex Wireless Communication*. Mobicom 2010.



- Device Cancellation

Place antennas at opposite sides of the device



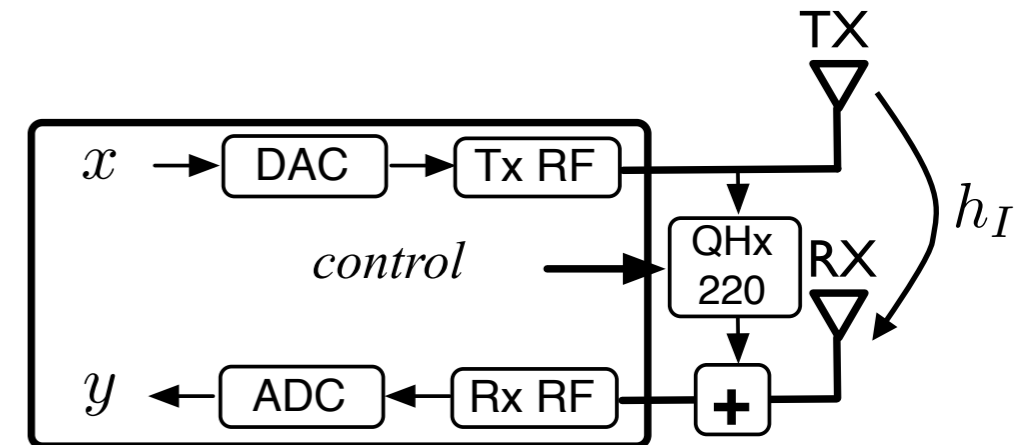
Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.





# Active Analog Cancellation

- Using QHx220 chip
- Tuning algorithm to control gain and delay that chip applies to its input
- Suitable for wideband frequency flat  $h_I$

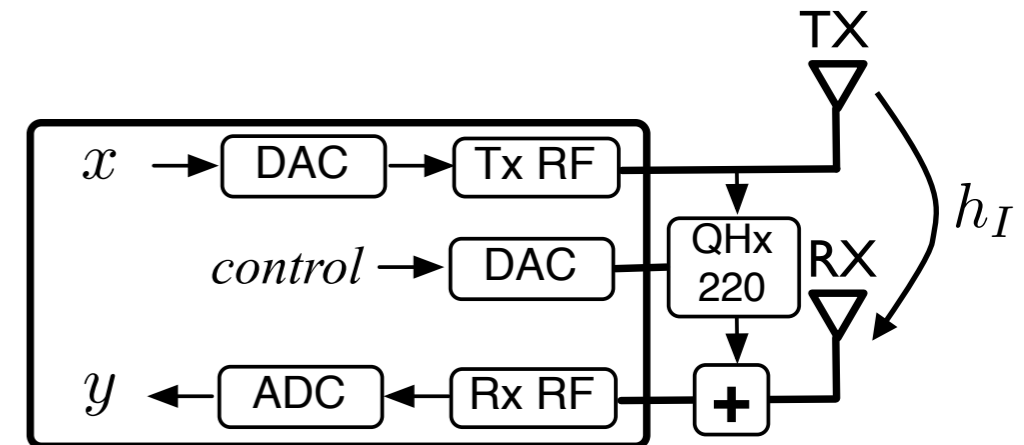


- Choi et al. *Achieving Single Channel, Full Duplex Wireless Communication*. Mobicom 2010.
- Radunovic et al. *Rethinking Indoor Wireless: Low Power, Low Frequency, Full-Duplex*. Tech. Report Microsoft Research 2009.

- Using extra Tx RF chain (without a power amplifier)

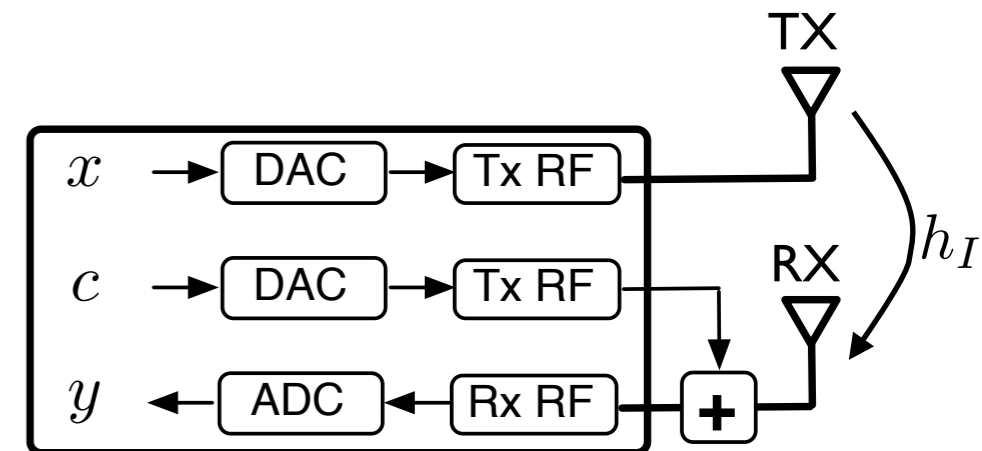
# Active Analog Cancellation

- Using QHx220 chip
- Tuning algorithm to control gain and delay that chip applies to its input
- Suitable for wideband frequency flat  $h_I$



- Choi et al. *Achieving Single Channel, Full Duplex Wireless Communication*. Mobicom 2010.
- Radunovic et al. *Rethinking Indoor Wireless: Low Power, Low Frequency, Full-Duplex*. Tech. Report Microsoft Research 2009.

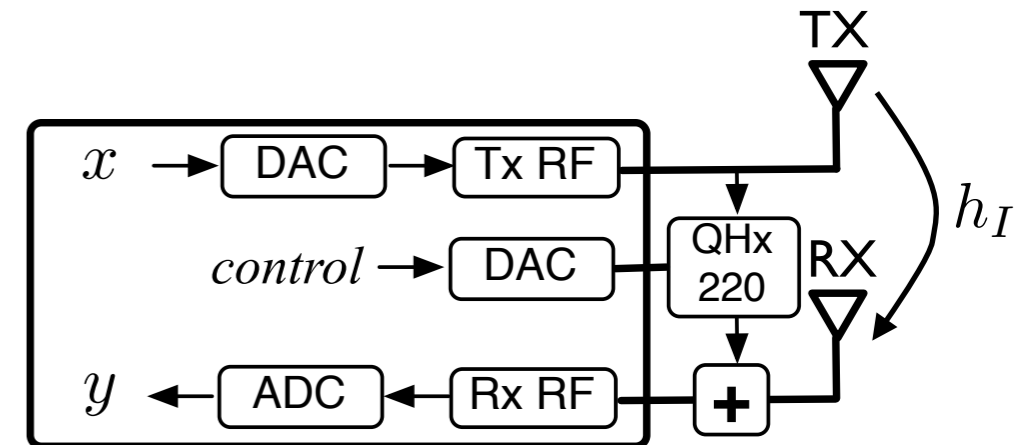
- Using extra Tx RF chain (without a power amplifier)
- Estimate  $h_I$  and design  $c$  for analog cancellation
- Suitable for wideband frequency flat **and frequency selective**  $h_I$
- **Uses off-the-shelf MIMO radios**



- Duarte et al. *Full-Duplex Wireless Communications using Off-The-Shelf Radios: Feasibility and First Results*. Asilomar 2010.
- Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.

# Active Analog Cancellation

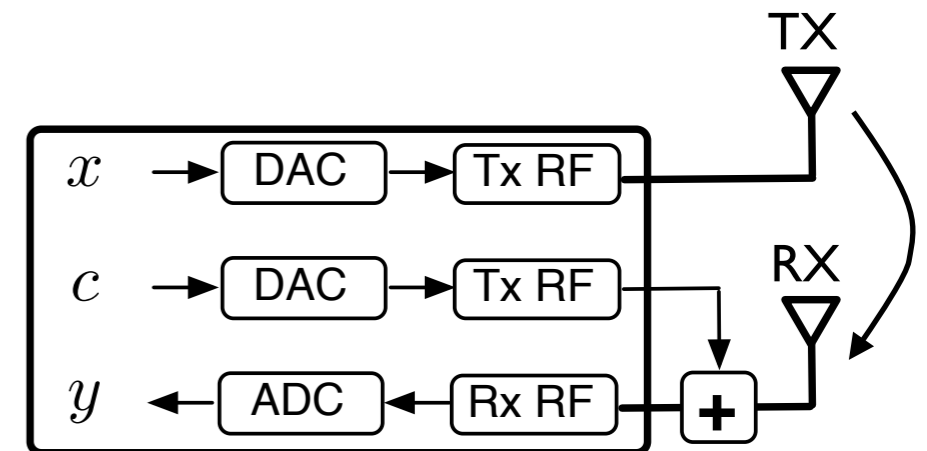
- Using QHx220 chip
- Tuning algorithm to control gain and delay that chip applies to its input
- Suitable for wideband frequency flat  $h_I$



- Choi et al. *Achieving Single Channel, Full Duplex Wireless Communication*. Mobicom 2010.
- Radunovic et al. *Rethinking Indoor Wireless: Low Power, Low Frequency, Full-Duplex*. Tech. Report Microsoft Research 2009.

- Used in our experiments

- Using extra Tx RF chain (without a power amplifier)
- Estimate  $h_I$  and design  $c$  for analog cancellation
- Suitable for wideband frequency flat **and frequency selective**  $h_I$
- **Uses off-the-shelf MIMO radios**



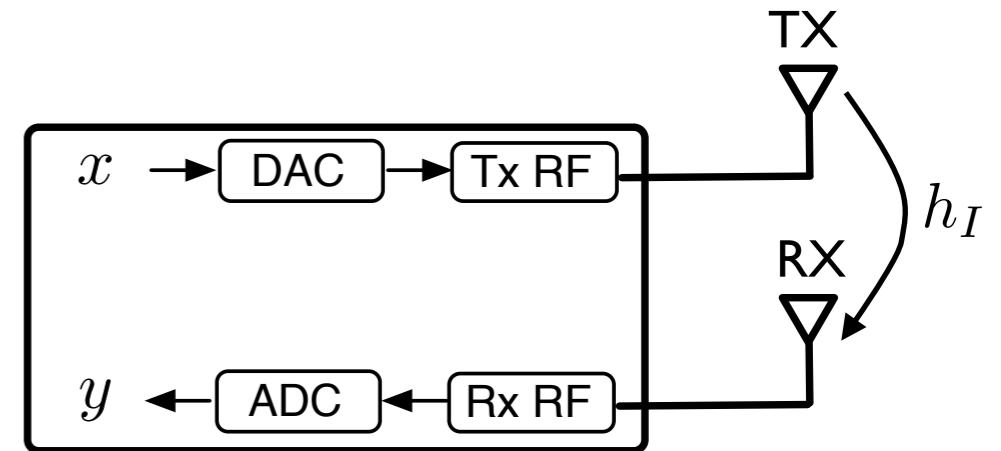
- Duarte et al. *Full-Duplex Wireless Communications using Off-The-Shelf Radios: Feasibility and First Results*. Asilomar 2010.
- Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.

# Active Digital Cancellation

- Without analog cancellation
- Combined with analog cancellation

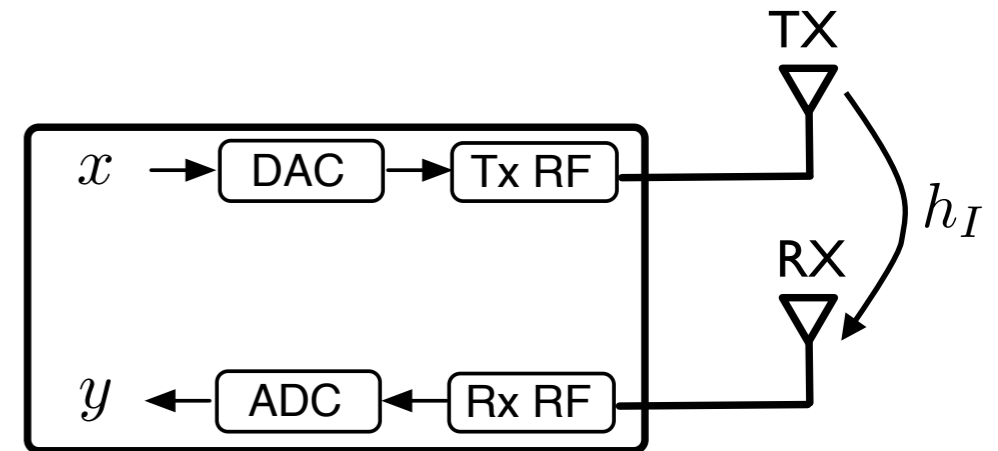
# Active Digital Cancellation

- Without analog cancellation
- Estimate  $h_I$  and cancel  $h_I x$  in the digital domain
- Combined with analog cancellation

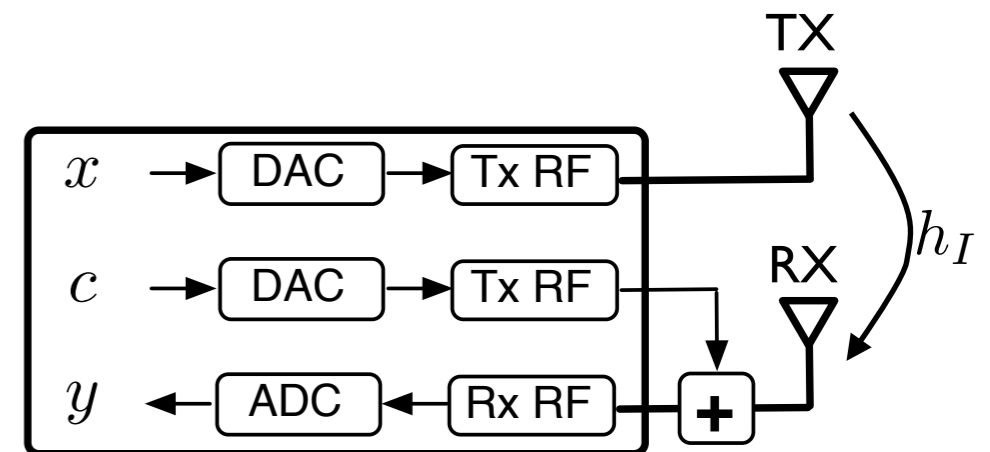


# Active Digital Cancellation

- Without analog cancellation
- Estimate  $h_I$  and cancel  $h_I x$  in the digital domain

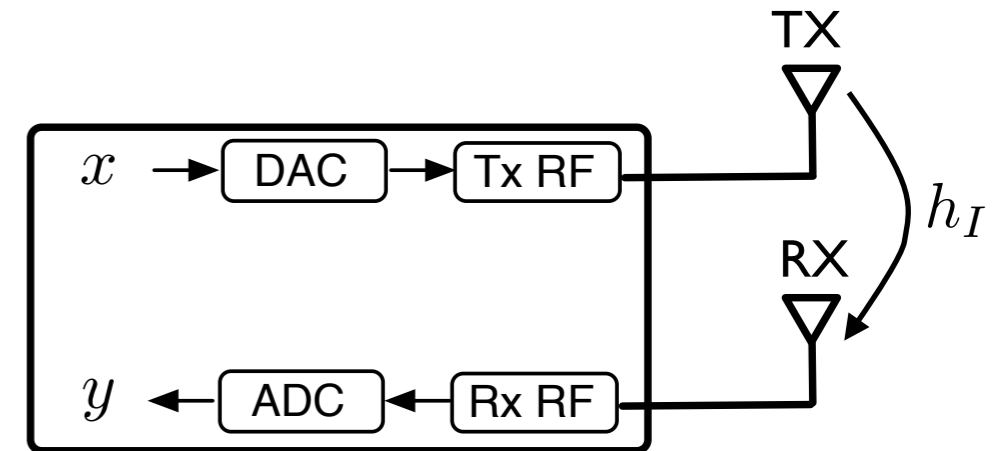


- Combined with analog cancellation
- Estimate residual interference and cancel in the digital domain

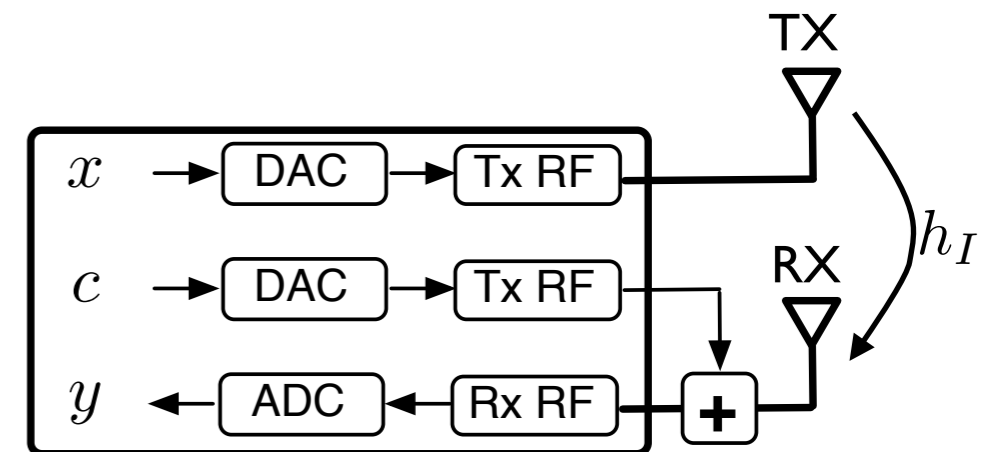


# Active Digital Cancellation

- Without analog cancellation
- Estimate  $h_I$  and cancel  $h_I x$  in the digital domain



- Combined with analog cancellation
- Estimate residual interference and cancel in the digital domain



- We have considered the two options above
- Allows us to characterize the effect in total cancellation when concatenating cancellation mechanisms
- Duarte et al. *Experiment-Driven Characterization of Full-duplex Wireless Systems*. Submitted to IEEE Trans. Wireless 2011.

# Full-Duplex Systems Considered

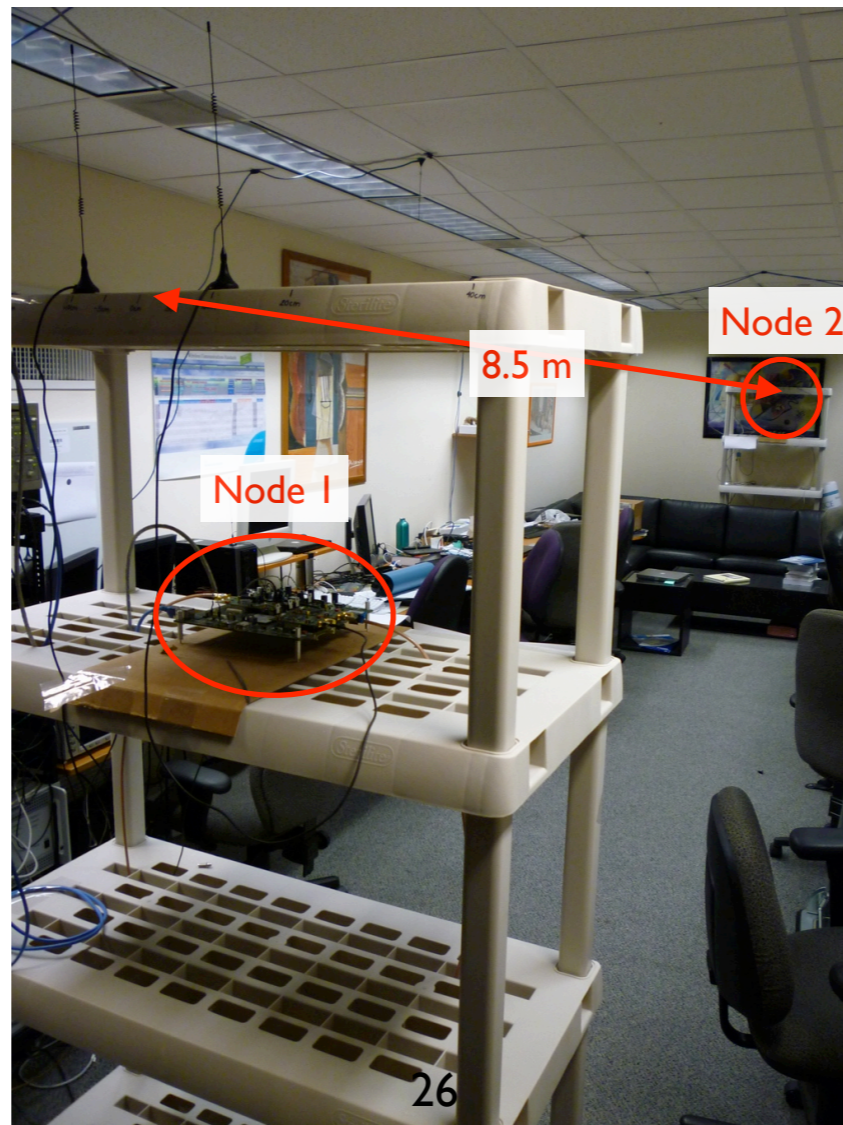
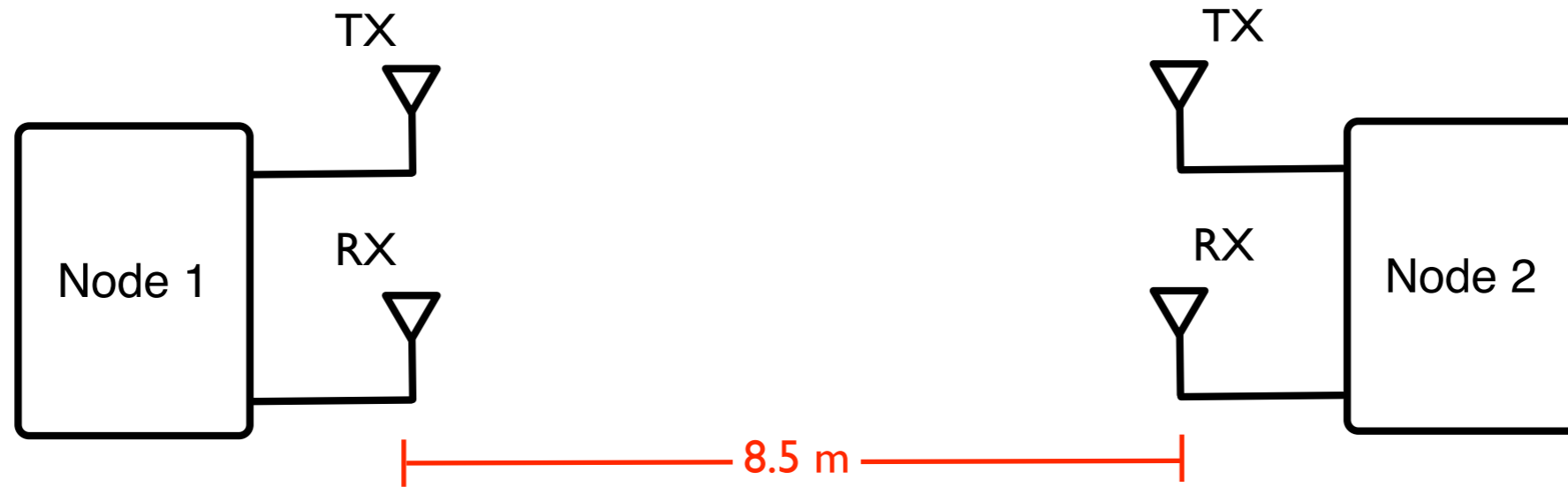
- We have implemented the following full-duplex systems
  - Antenna Separation + Digital Cancellation
  - Antenna Separation + Analog Cancellation
  - Antenna Separation + Analog Cancellation + Digital Cancellation



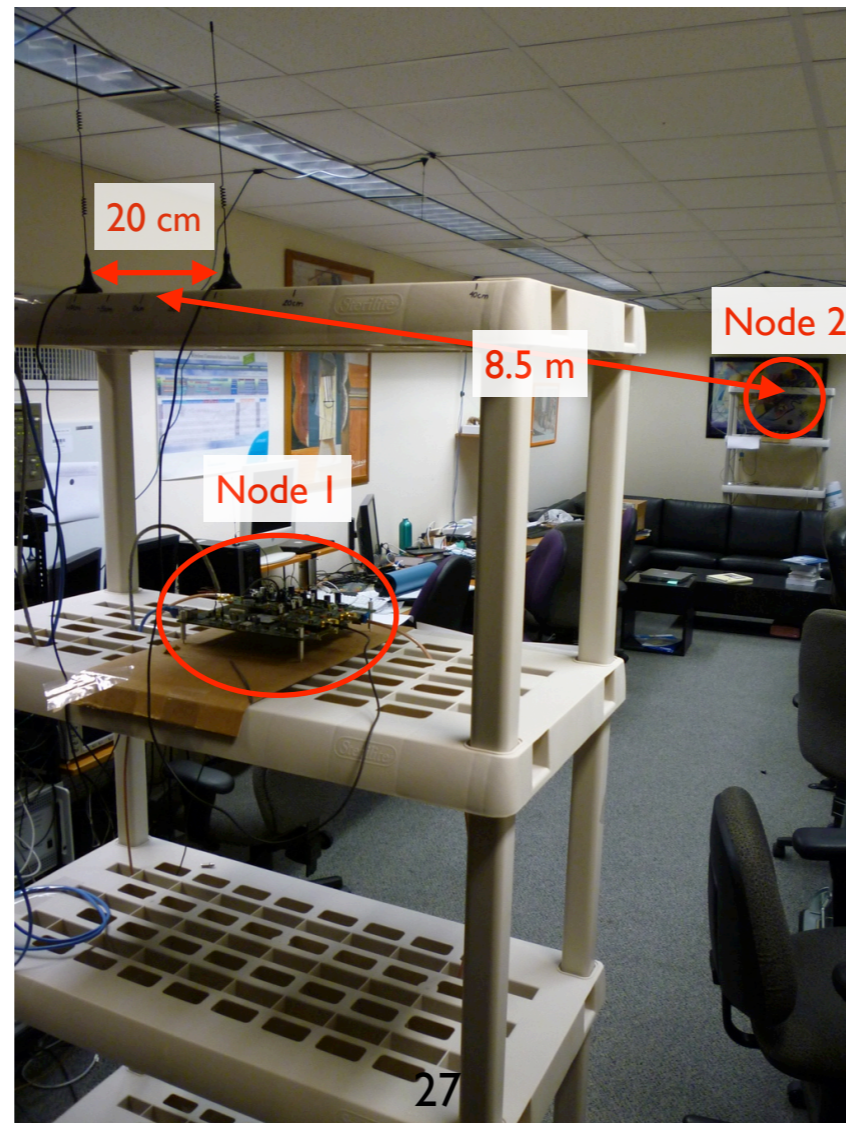
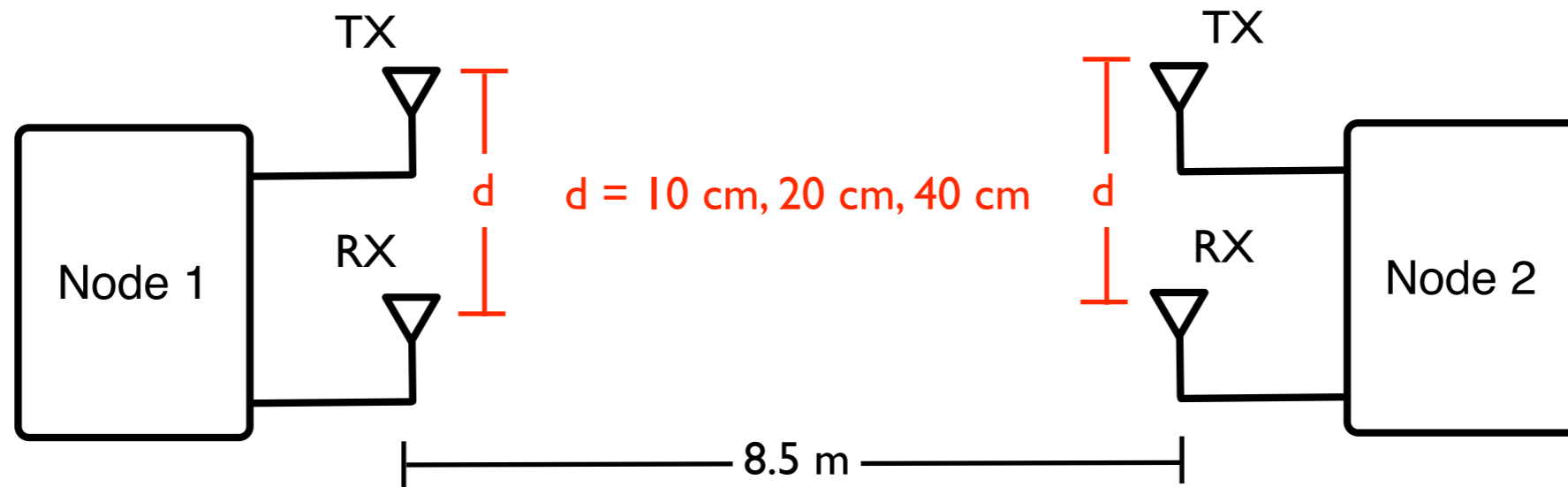
# Summary of Results

- Characterization of self-interference cancellation mechanisms
  - Amount of cancellation
  - Impact on full-duplex achievable rate performance
  
- Comparison with half-duplex systems
  - Demonstrated that full-duplex can achieve higher rates than half-duplex
  
- Duarte et al. *Full-Duplex Wireless Communications using Off-The-Shelf Radios: Feasibility and First Results*. Asilomar 2010.
- Duarte et al. *Experiment-Driven Characterization of Full-duplex Wireless Systems*. Submitted to IEEE Trans. Wireless 2011.

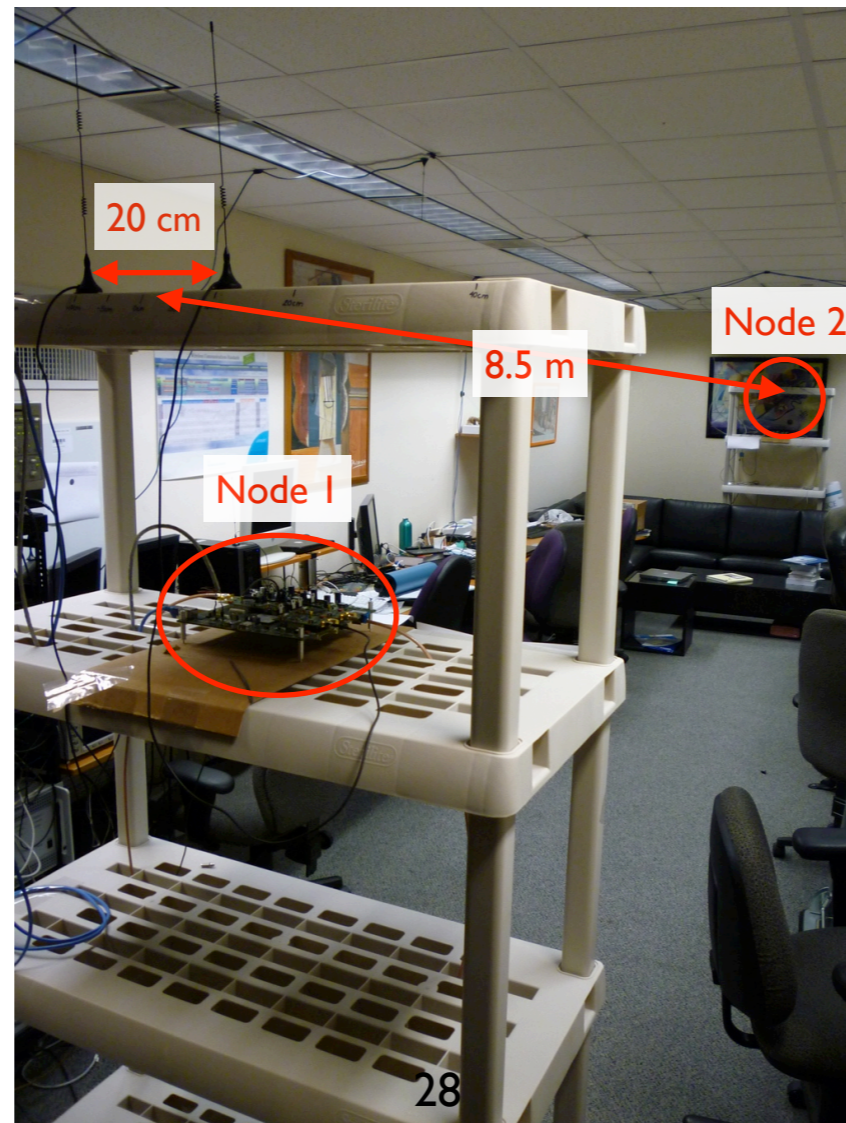
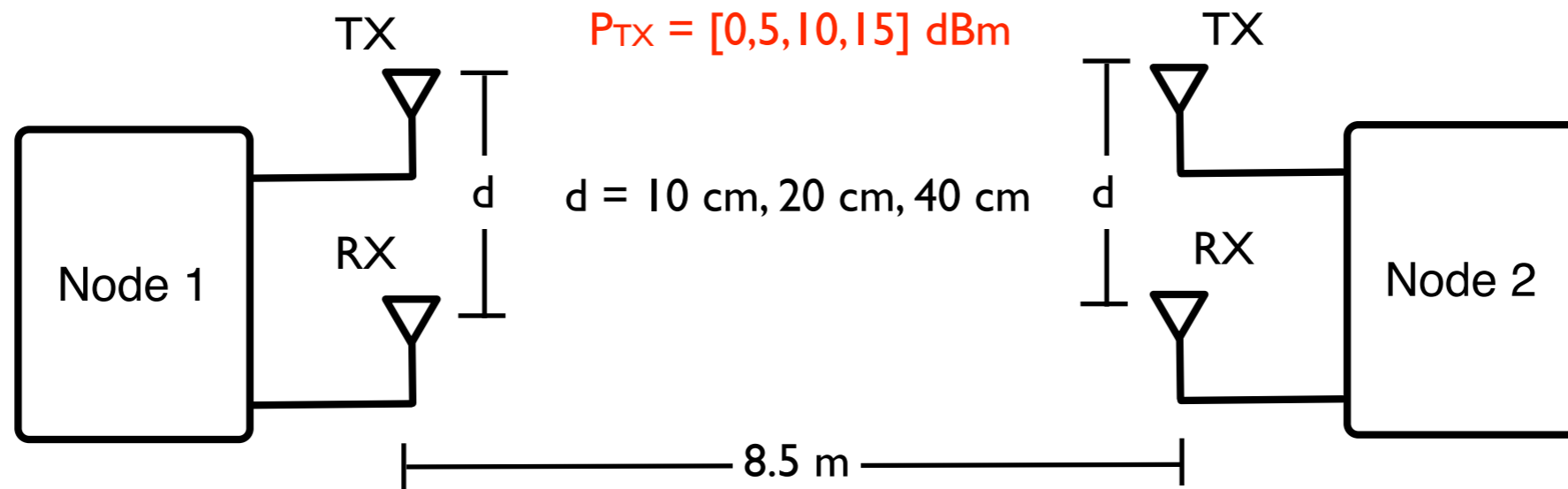
# Experiment Setup



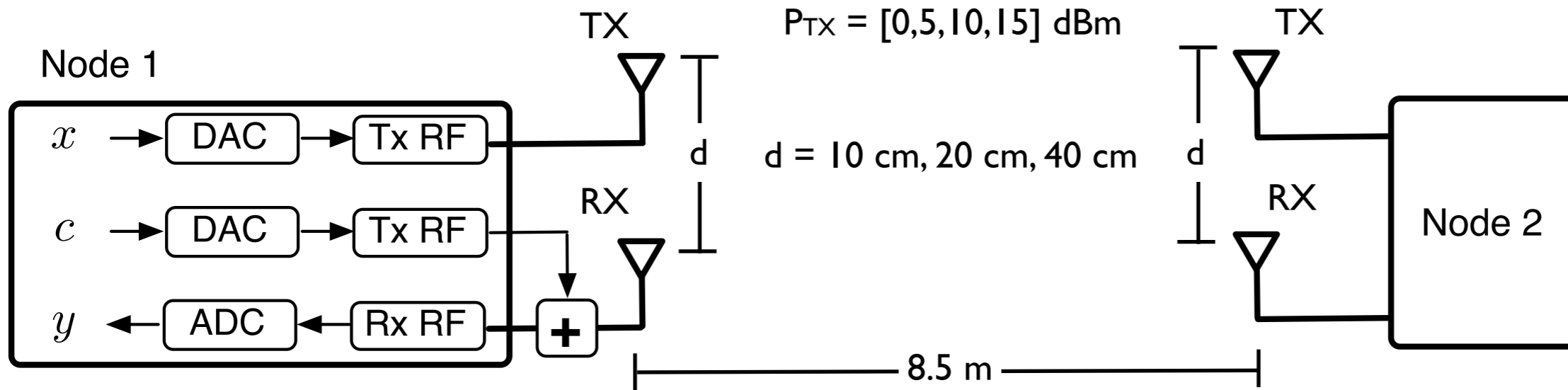
# Experiment Setup



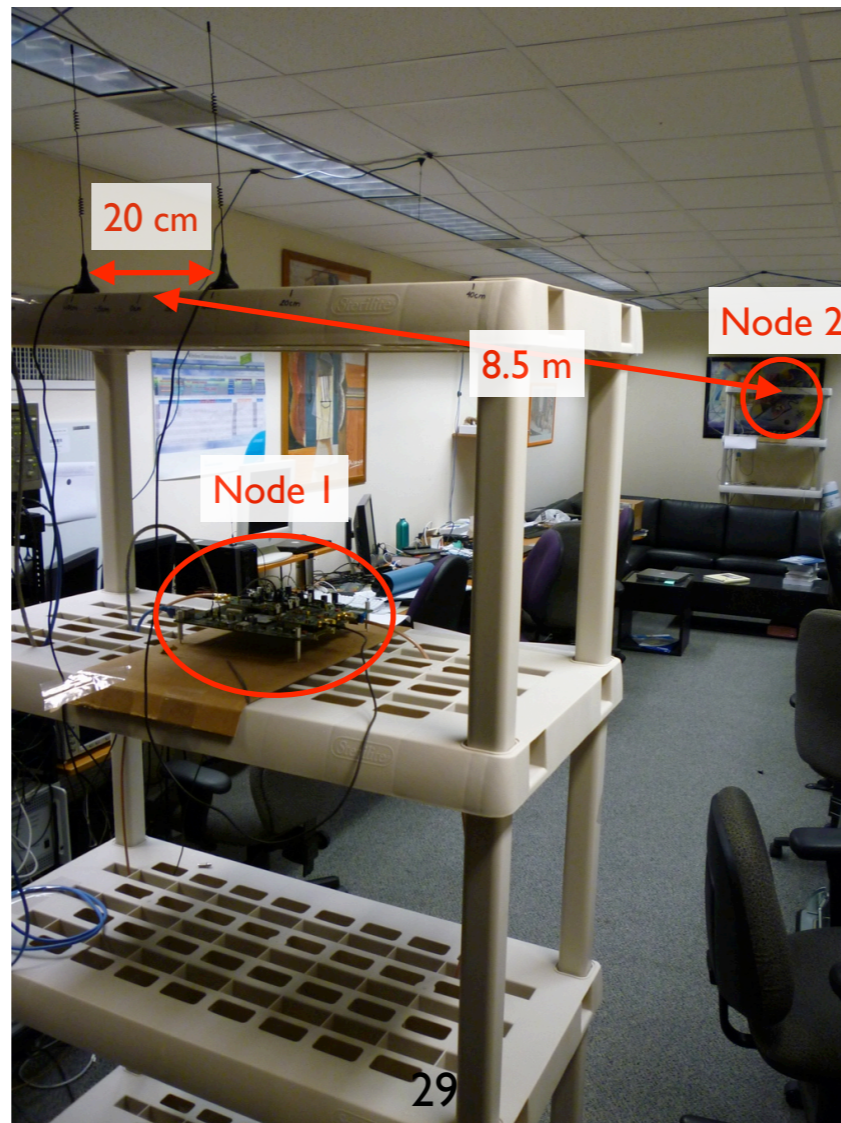
# Experiment Setup



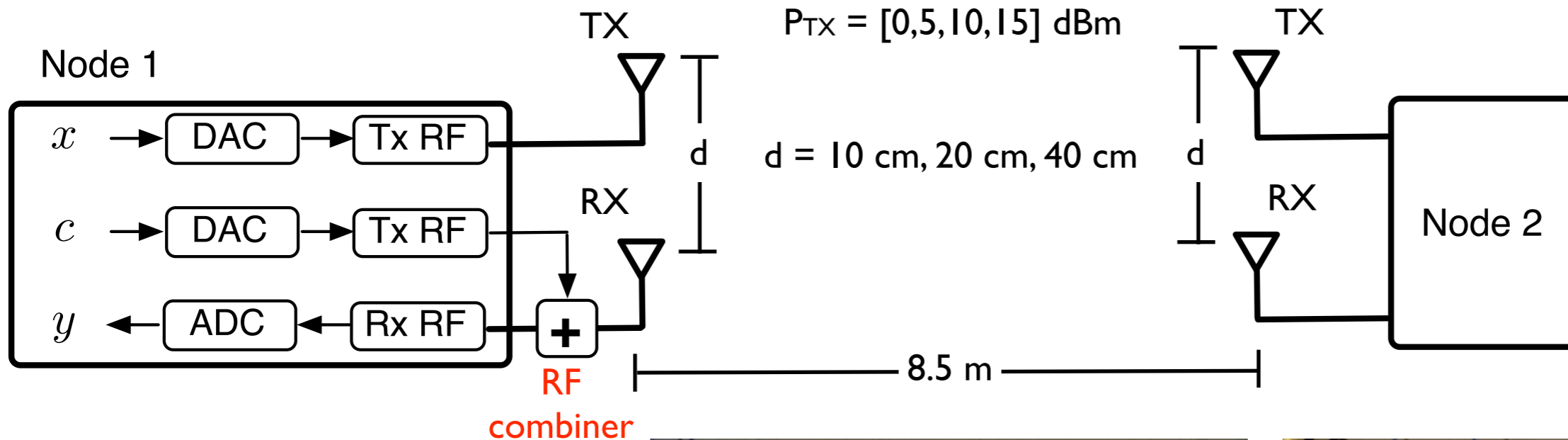
# Experiment Setup



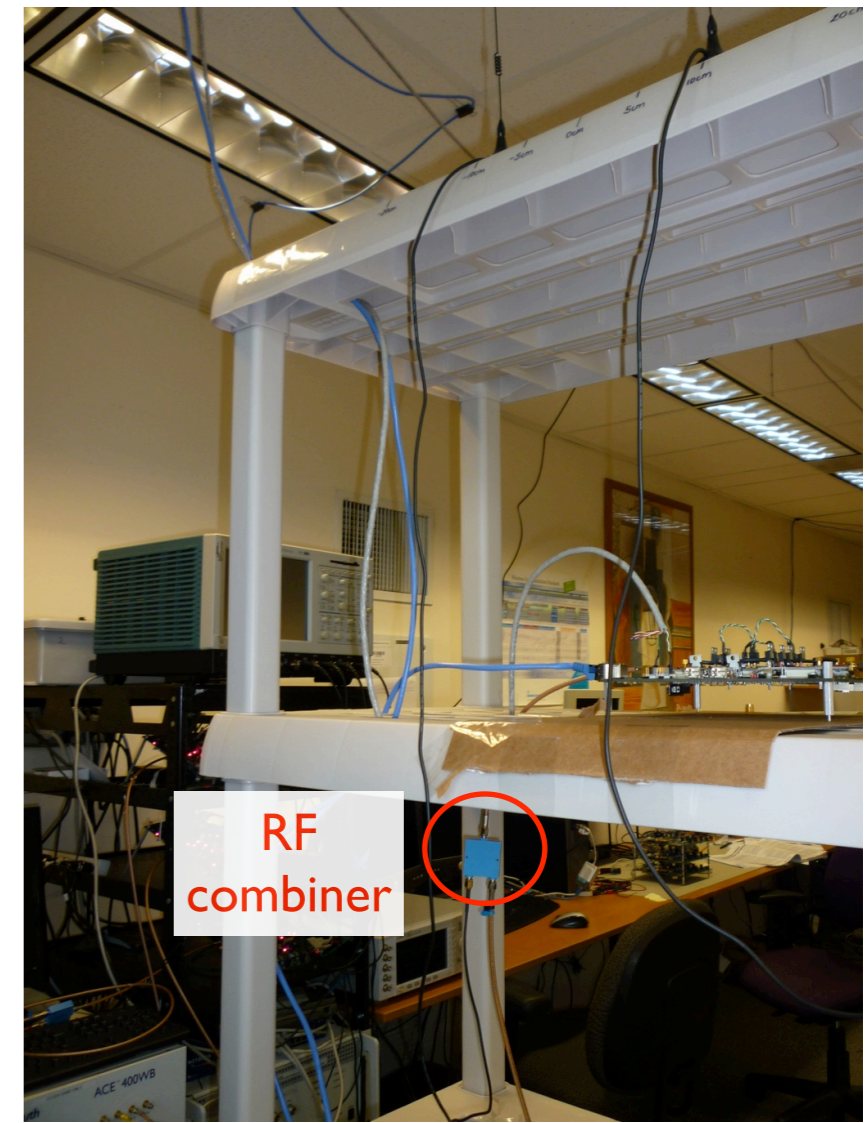
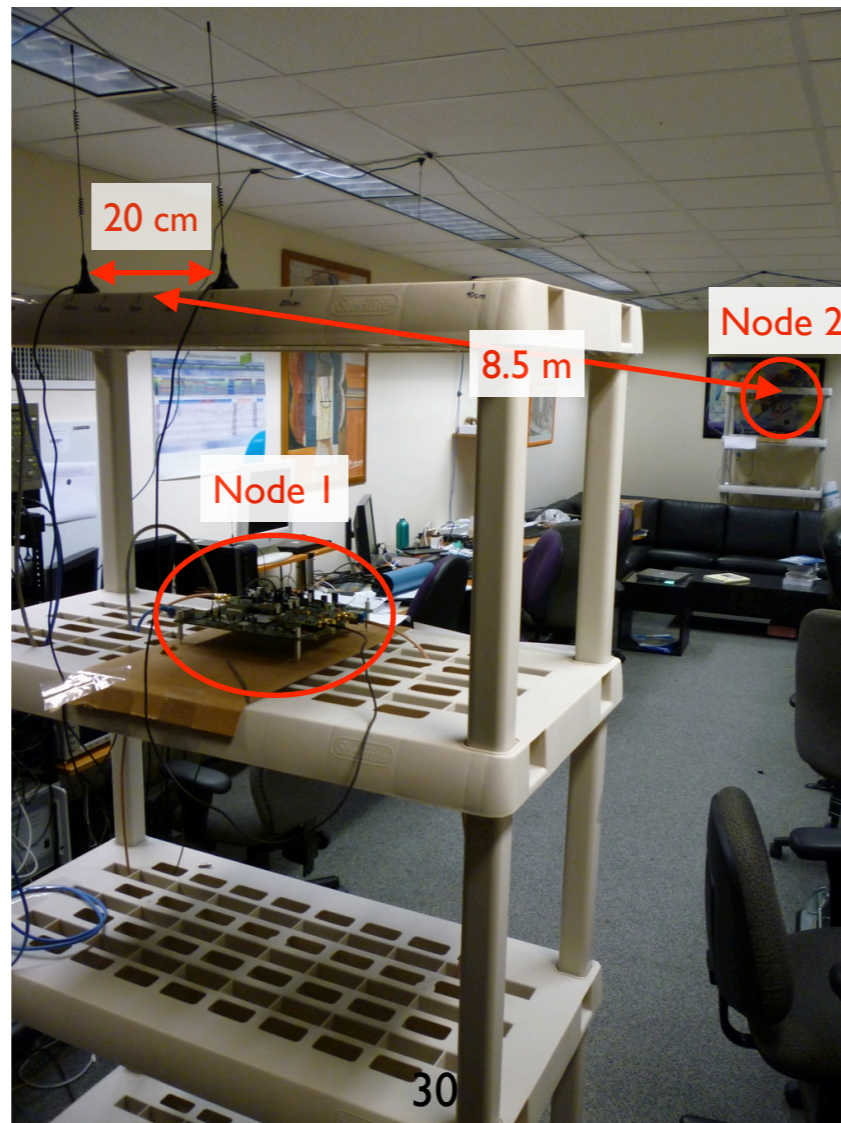
- WARP with 3 radios
- WARPLab = WARP + Matlab, to generate/analyze signals
- Narrowband tests, 0.65 MHz
- Recent extension to OFDM 10MHz @ Rice
  - Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.



# Experiment Setup



- WARP with 3 radios
- WARPLab = WARP + Matlab, to generate/analyze signals
- Narrowband tests, 0.65 MHz
- Recent extension to OFDM 10MHz @ Rice
- Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.

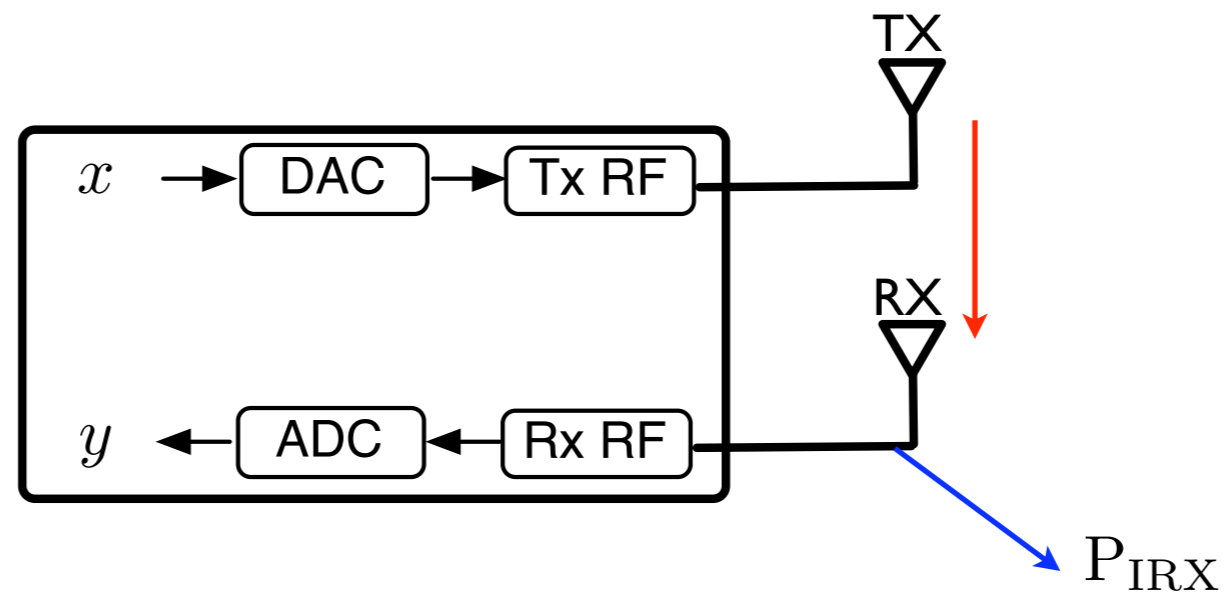


# Characterization of Average Cancellation

- Digital cancellation
- Analog cancellation
- Analog and digital cancellation

# Characterization of Average Cancellation

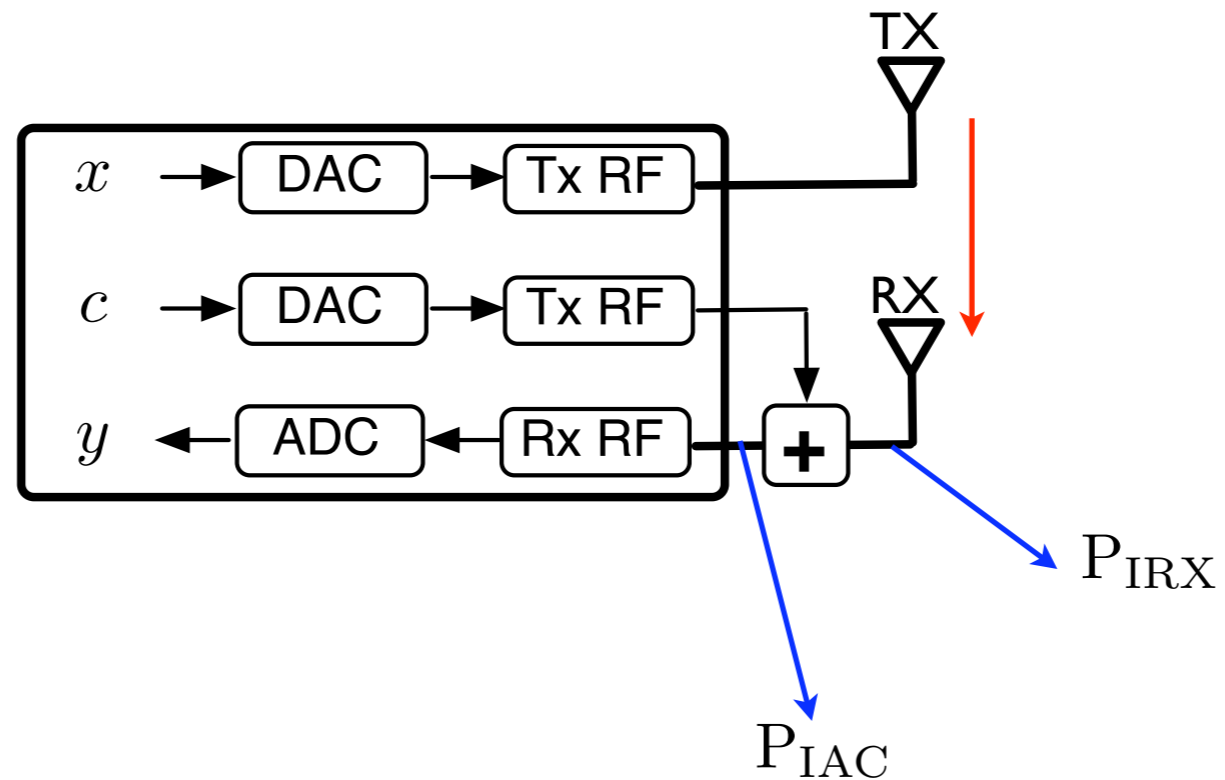
- Digital cancellation
- Analog cancellation
- Analog and digital cancellation





# Characterization of Average Cancellation

- Digital cancellation
- Analog cancellation
- Analog and digital cancellation



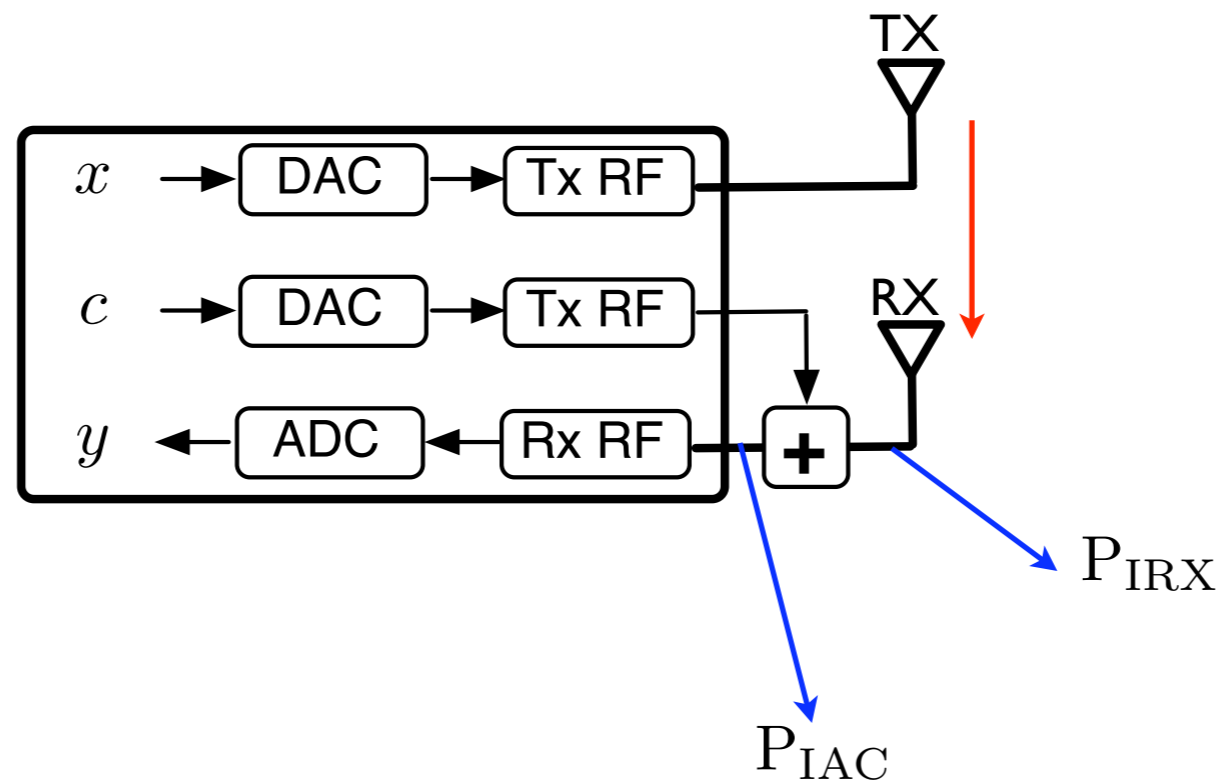
# Characterization of Average Cancellation

- Digital cancellation

- Analog cancellation

- Analog and digital cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



# Characterization of Average Cancellation

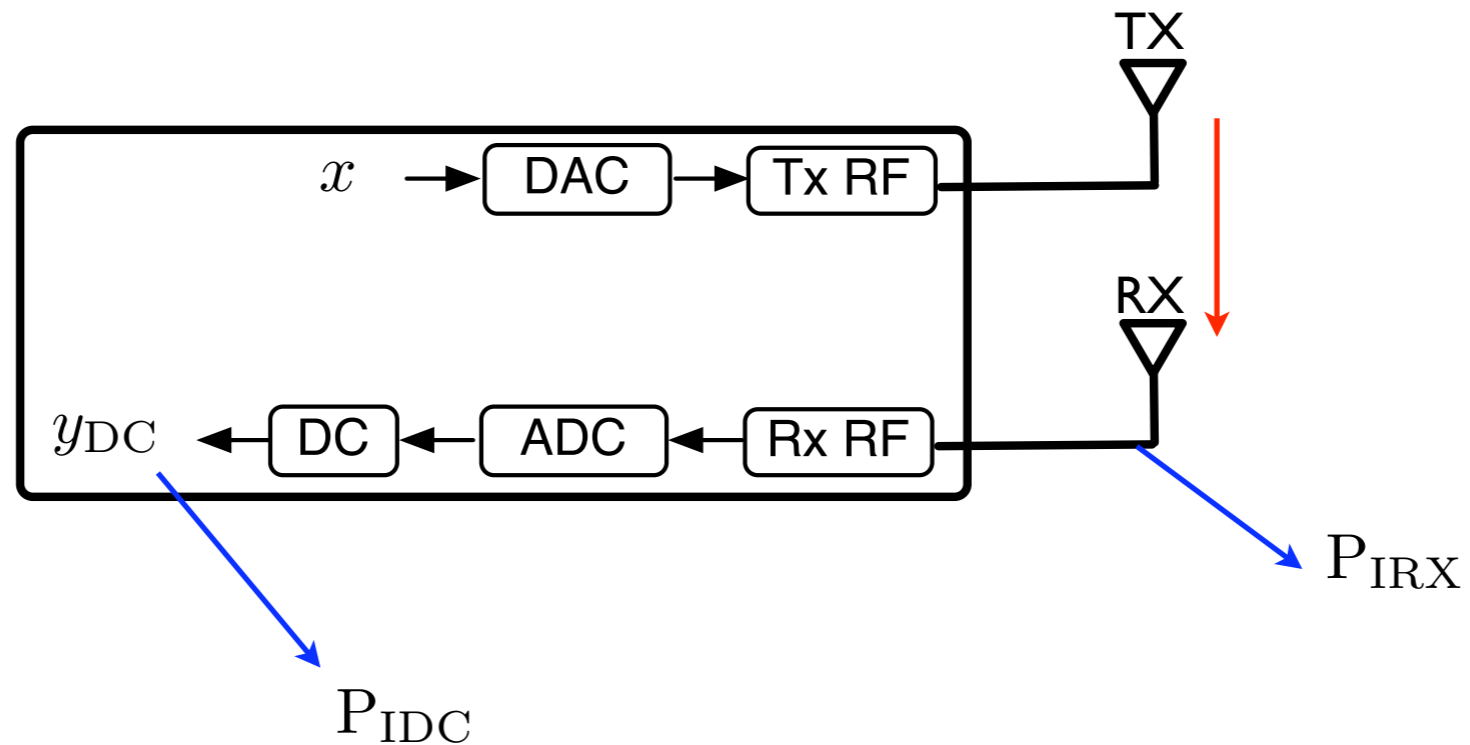
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$

- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$

- Analog and digital cancellation



# Characterization of Average Cancellation

- Digital cancellation

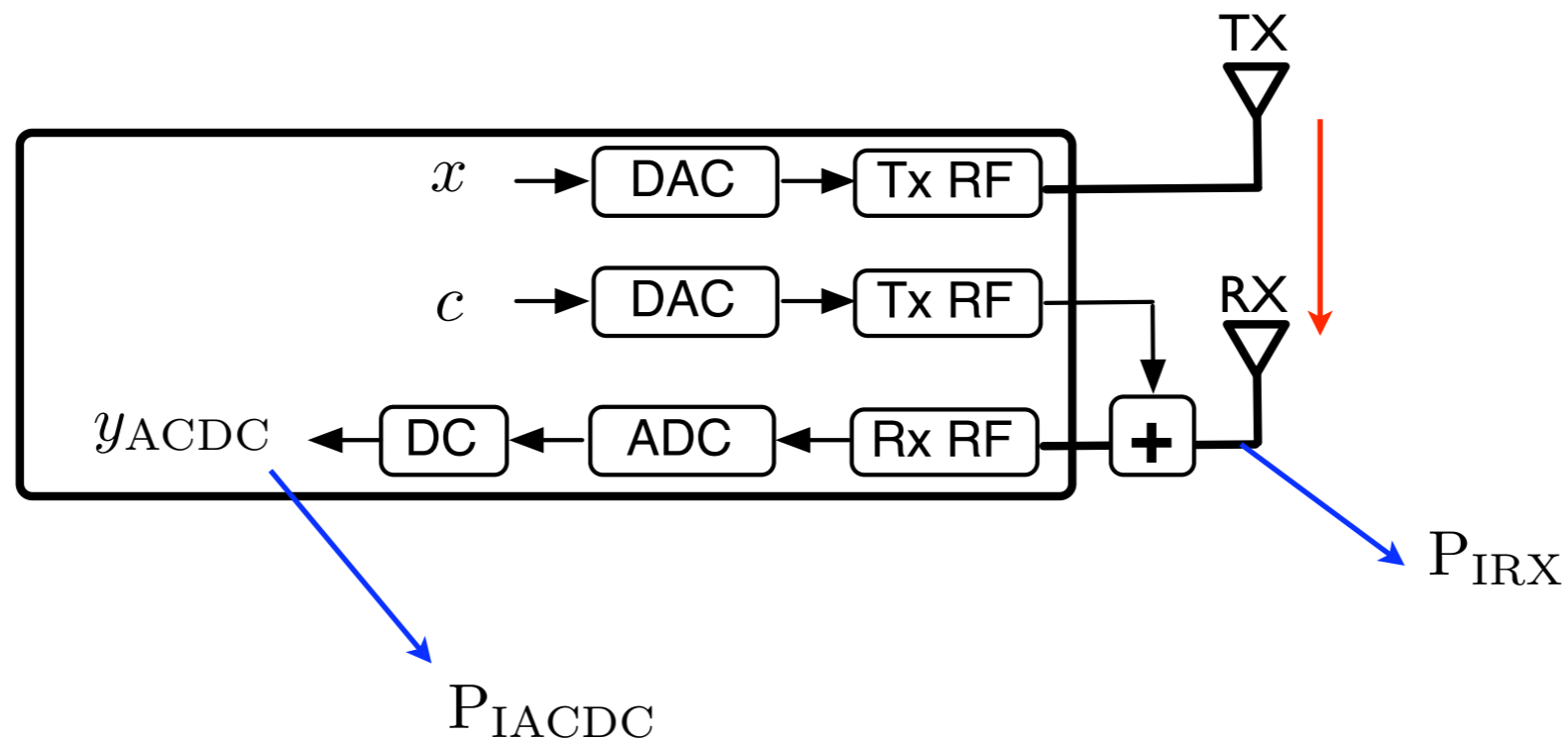
$$\alpha_{DC} = P_{IRX} - P_{IDC}$$

- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$

- Analog and digital cancellation

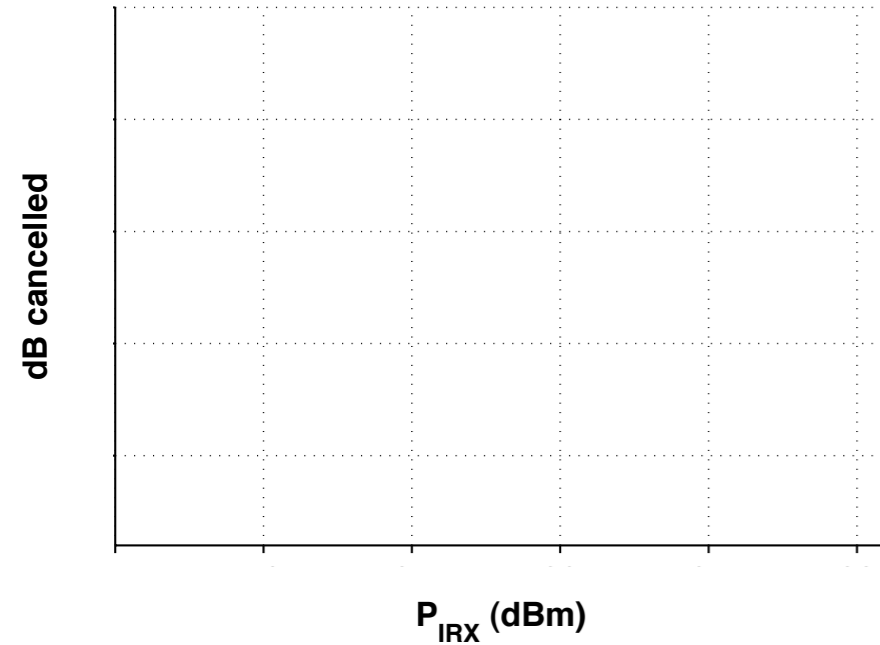
$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



# Characterization of Average Cancellation

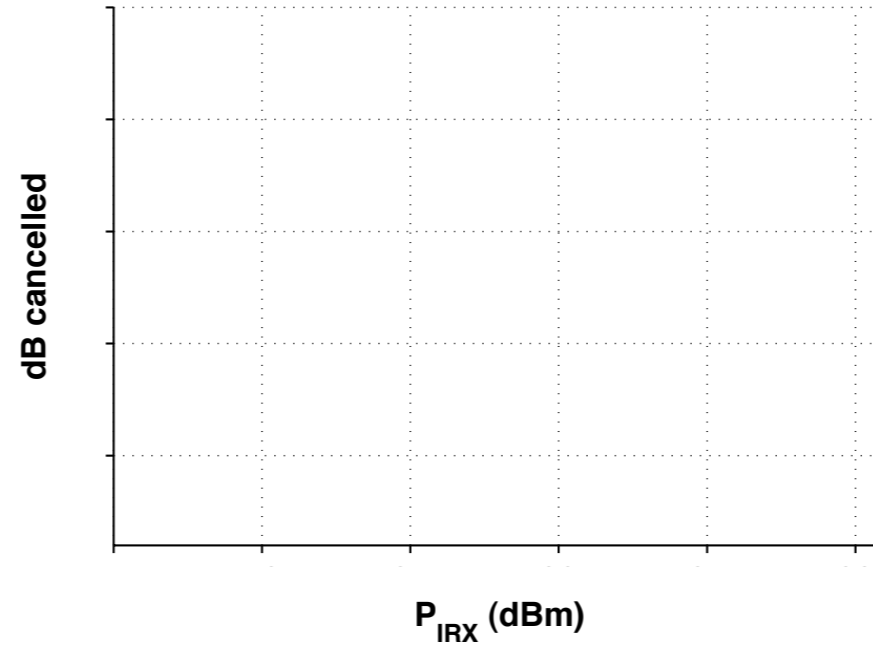
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



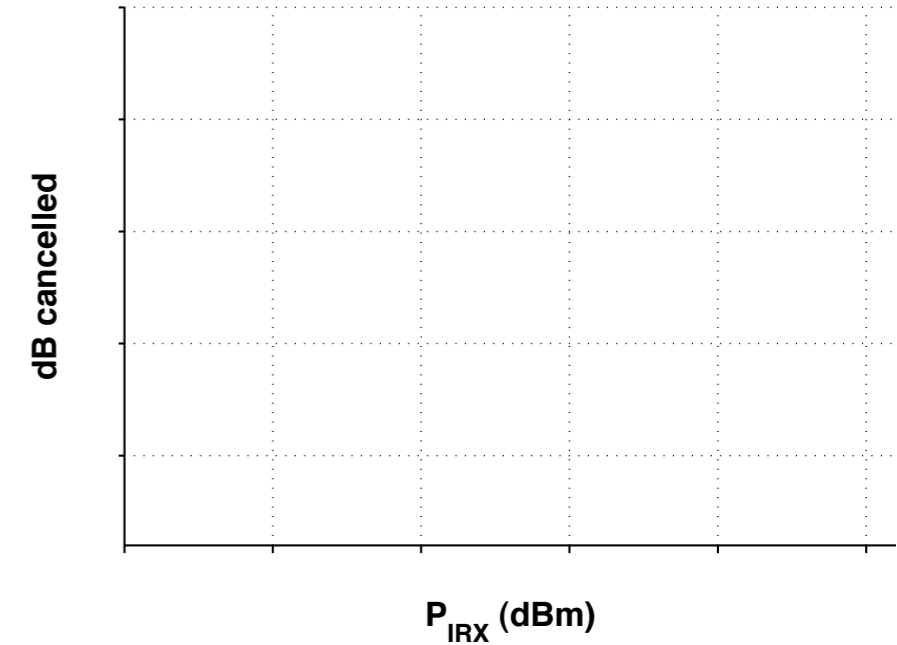
- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



- Analog and digital cancellation

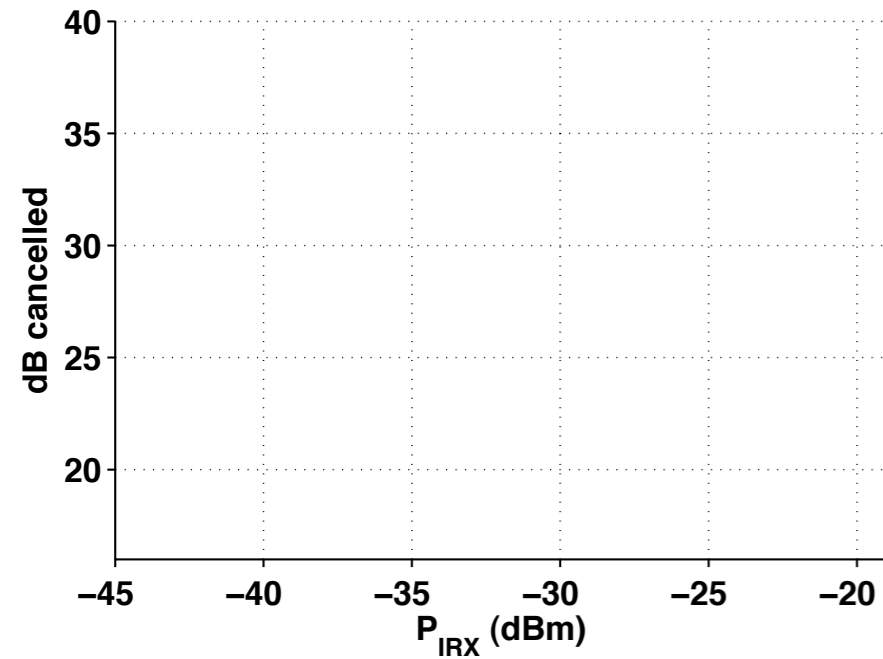
$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



# Characterization of Average Cancellation

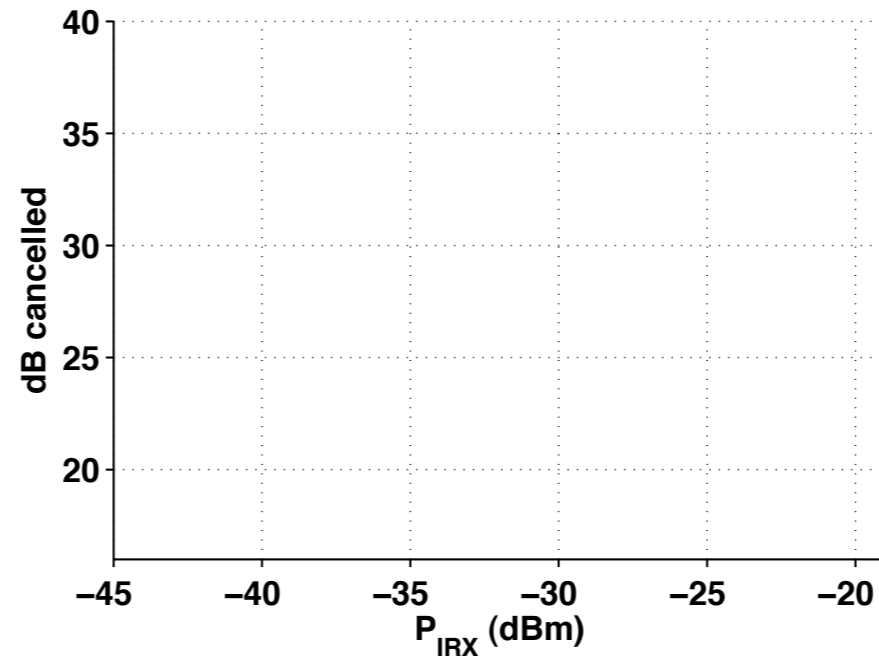
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



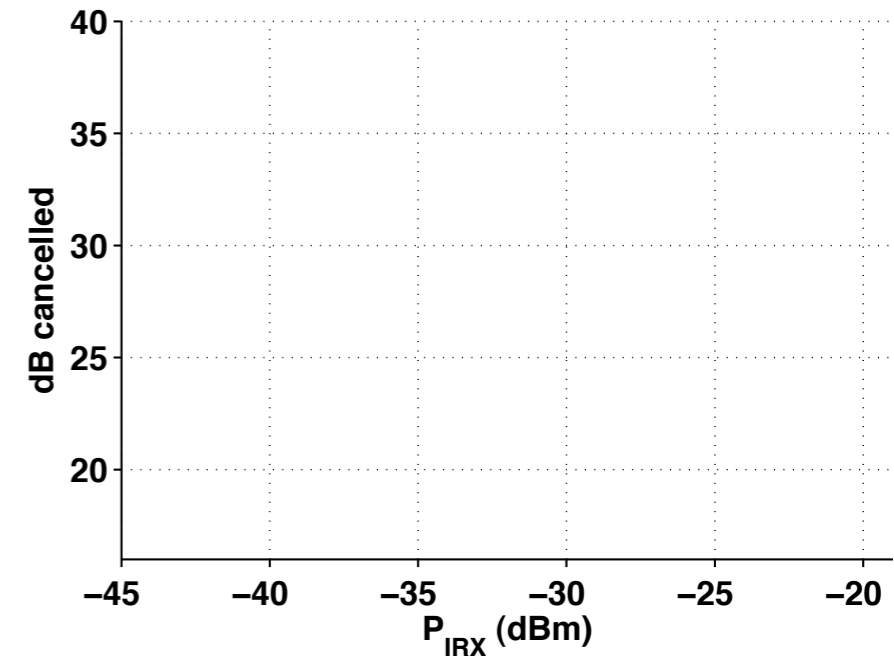
- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



- Analog and digital cancellation

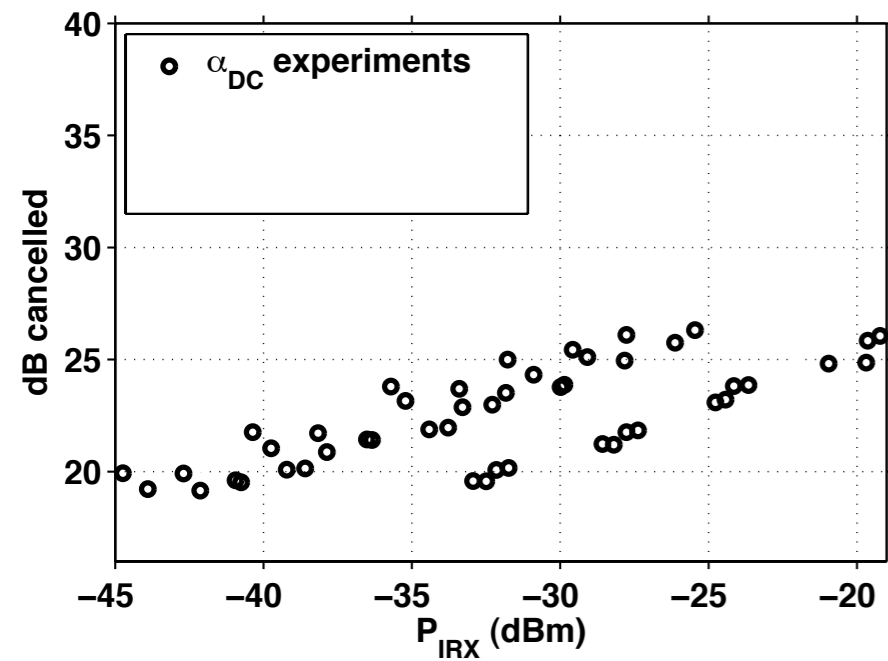
$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



# Characterization of Average Cancellation

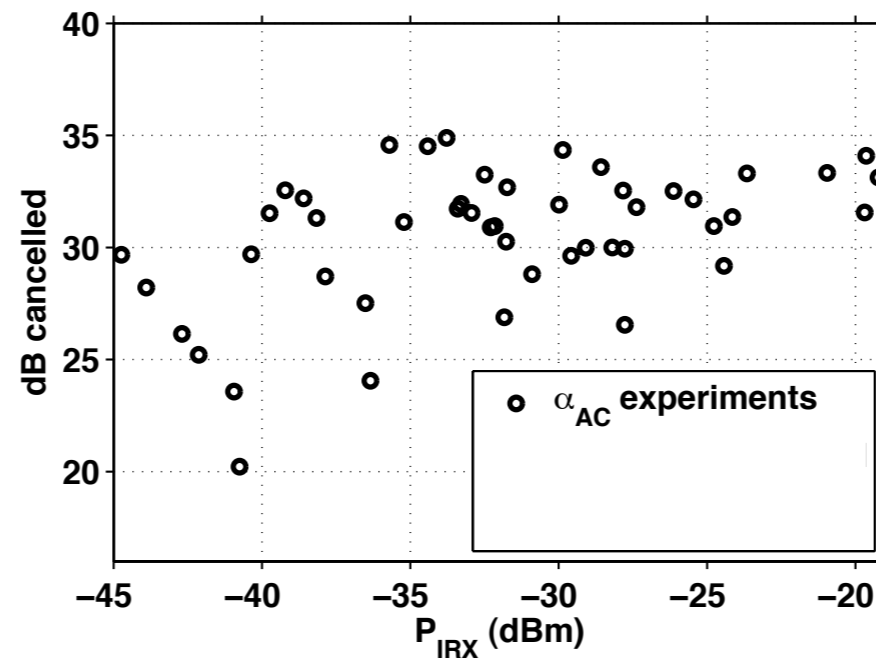
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



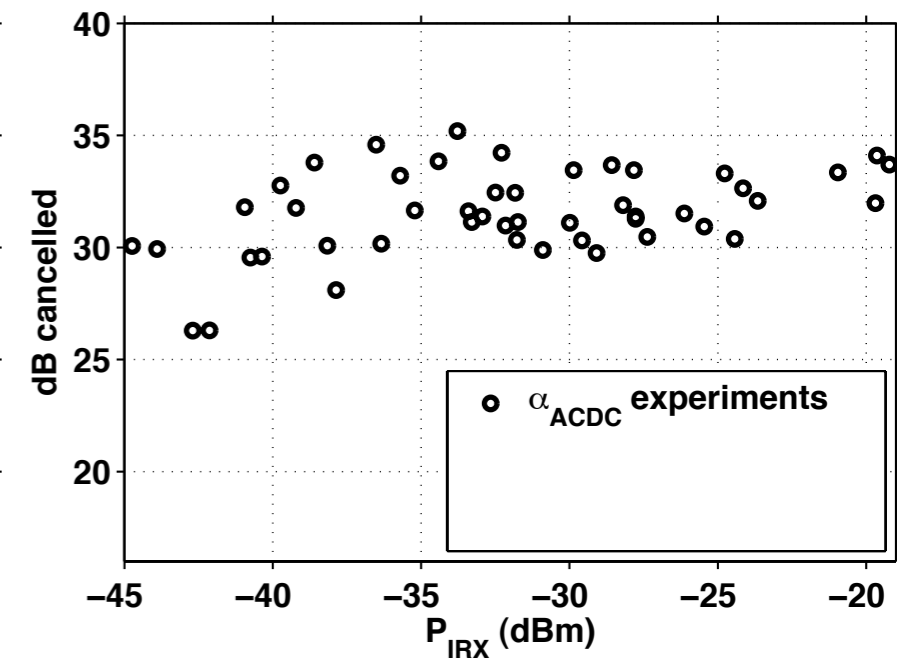
- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



- Analog and digital cancellation

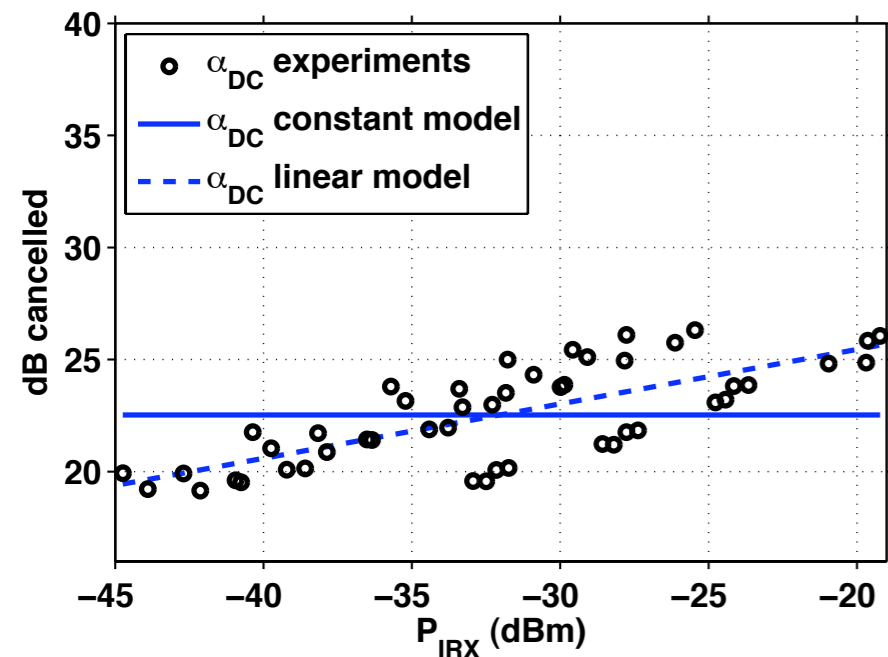
$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



# Characterization of Average Cancellation

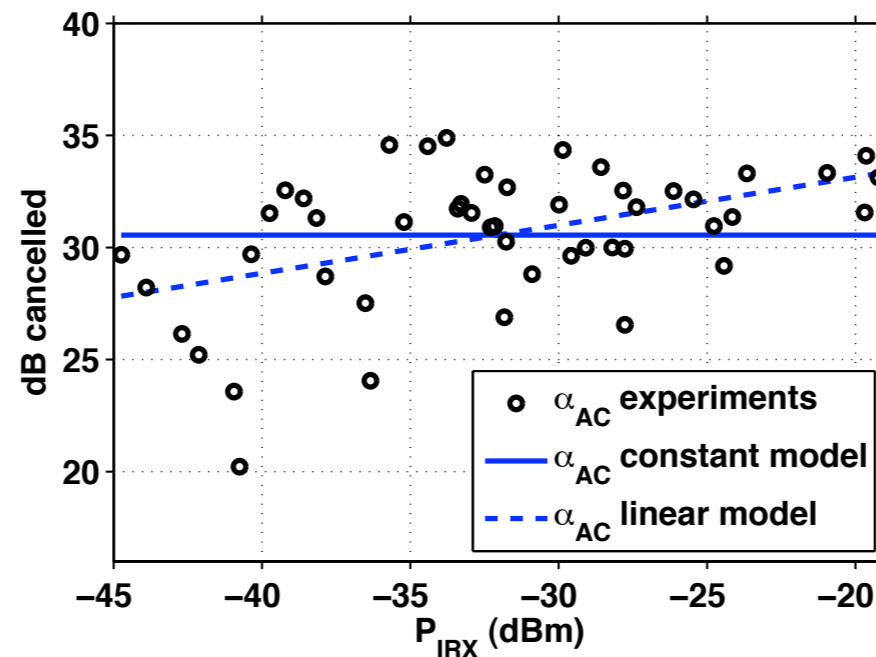
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



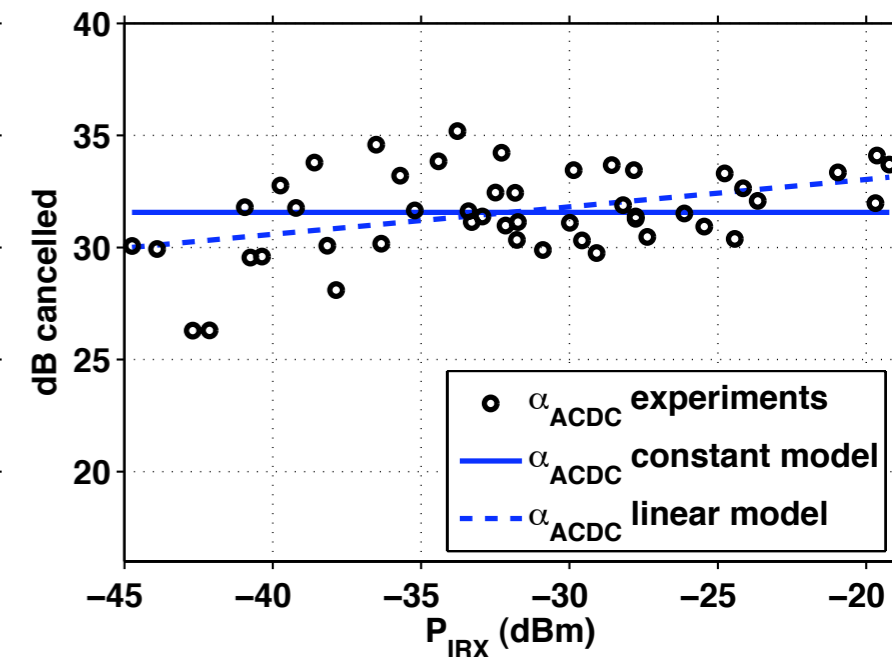
- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



- Analog and digital cancellation

$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



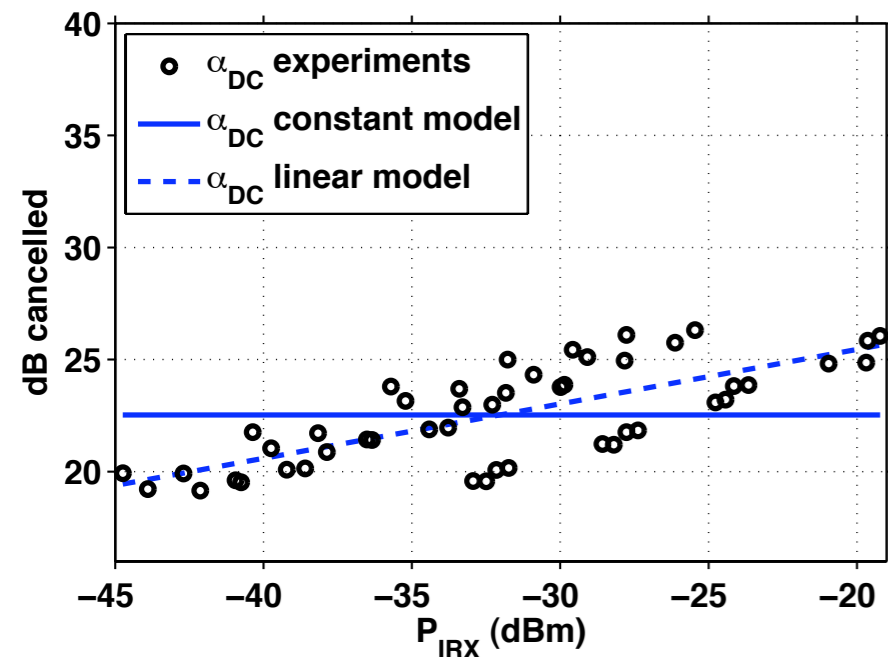
- We want a simple model for the average cancellation
  - Option 1: Fit the data to a constant model
  - Option 2: Fit the data to a linear model



# Characterization of Average Cancellation

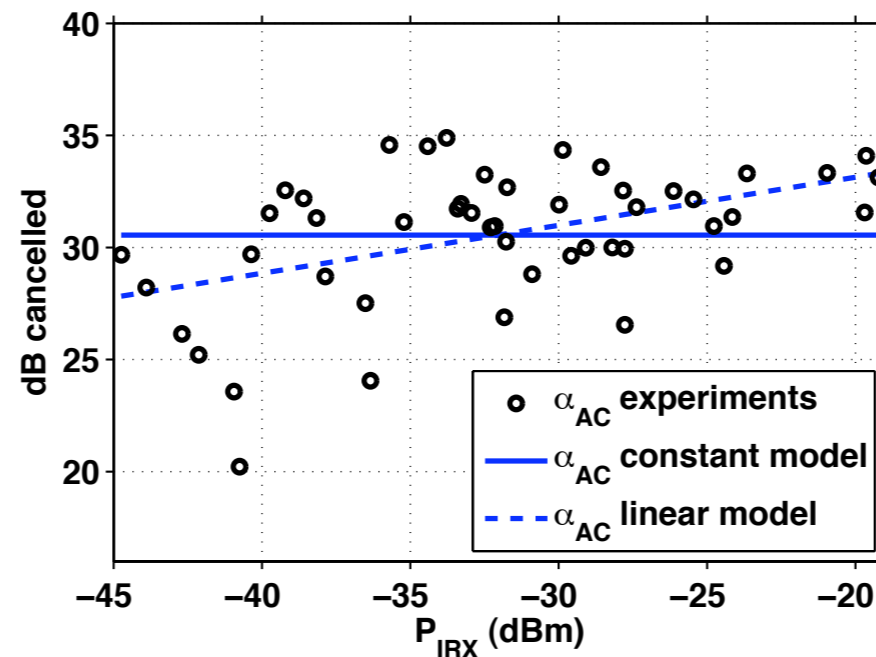
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



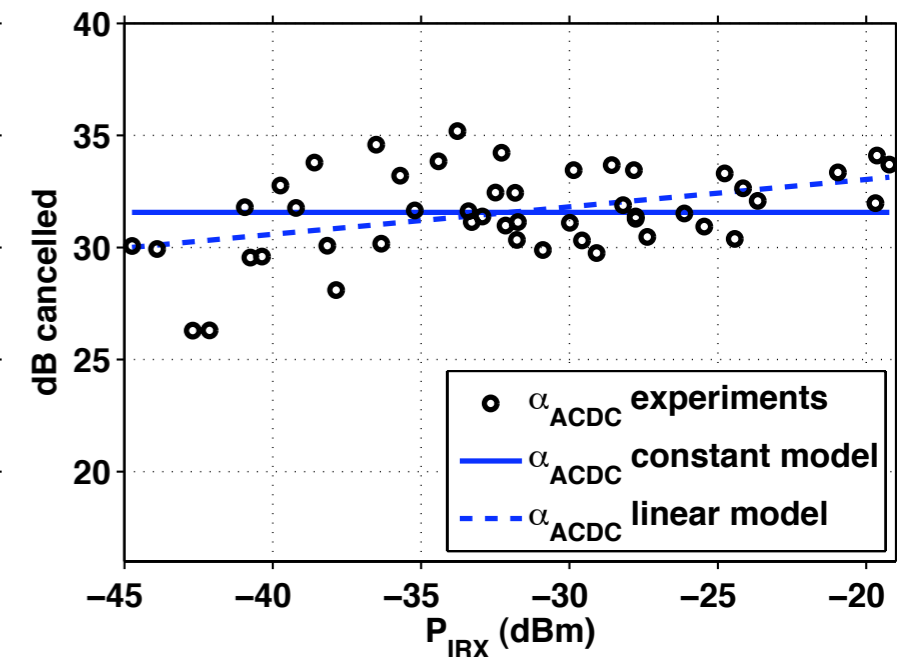
- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



- Analog and digital cancellation

$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



- Result I:

- As received interference power  $P_{IRX}$  increases amount of cancellation increases

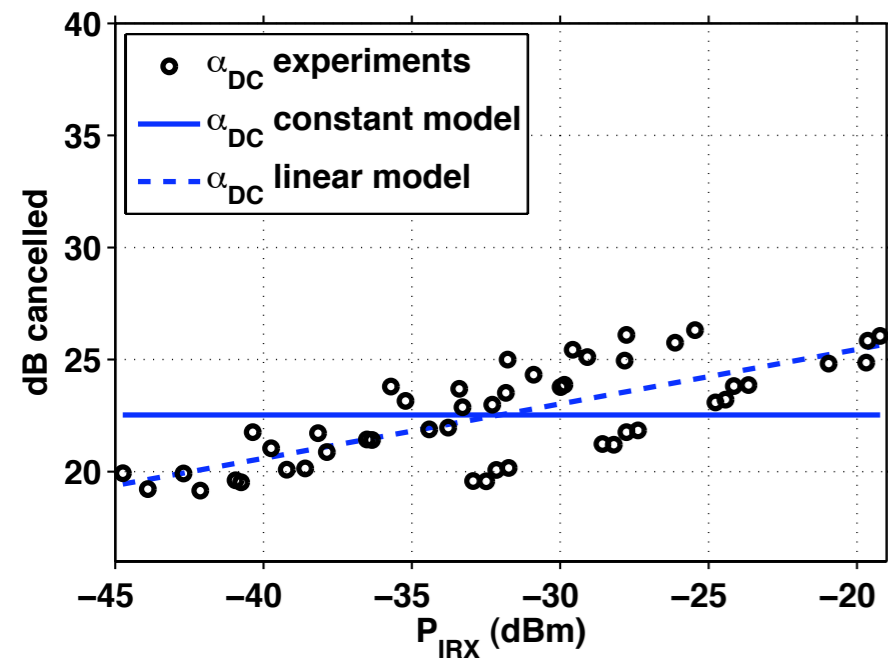
- Reason:

- Cancellation is based on channel measurement
- Higher  $P_{IRX}$  means higher SNR for channel estimation
- Better estimation and hence increased cancellation

# Characterization of Average Cancellation

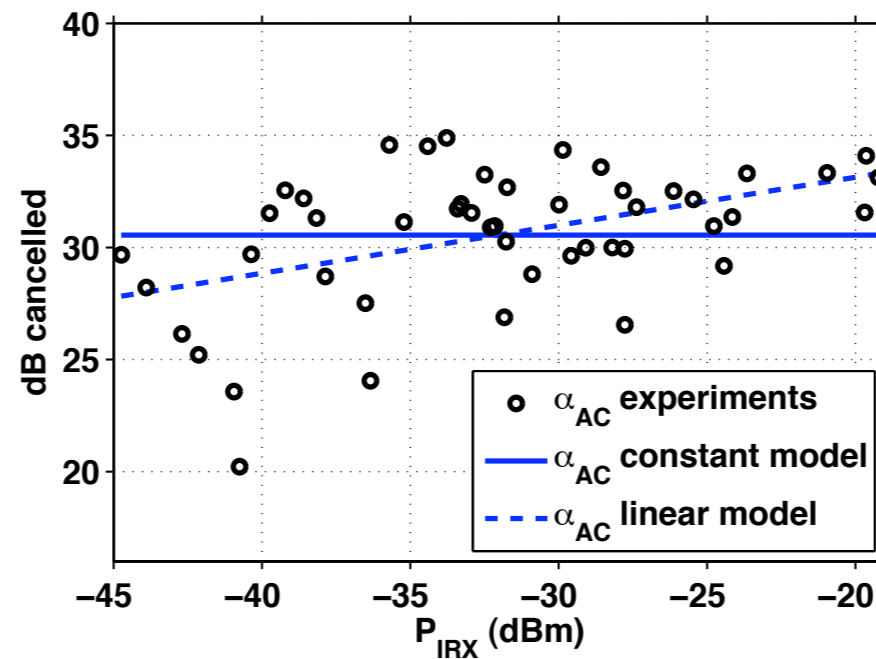
- Digital cancellation

$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



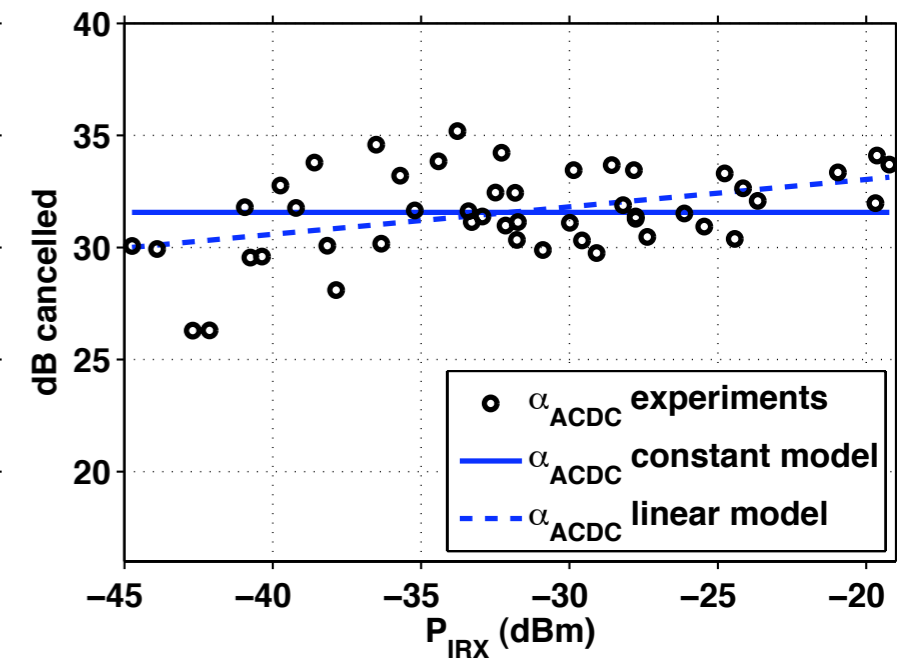
- Analog cancellation

$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



- Analog and digital cancellation

$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



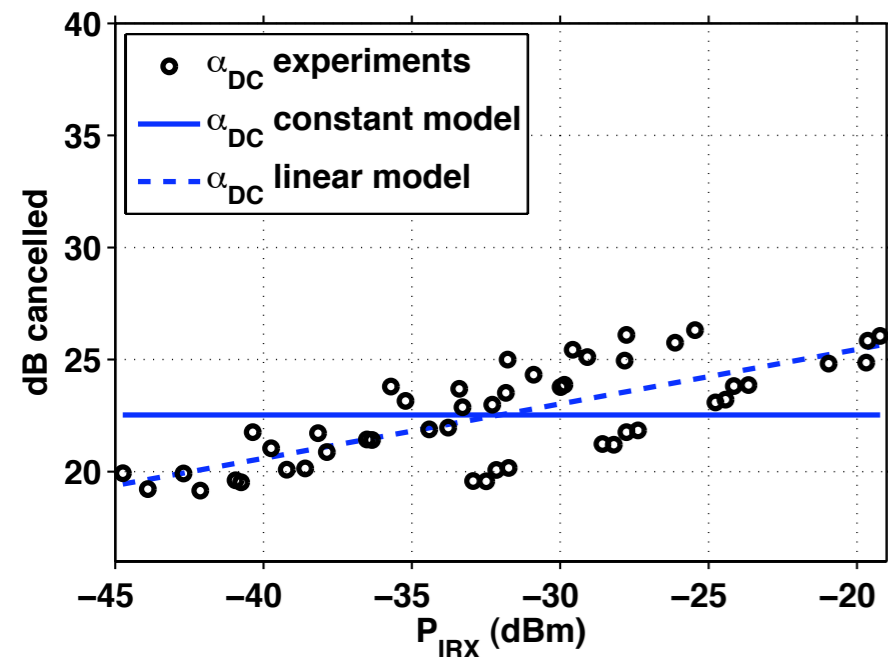
- Result 2:

(a) Concatenation of cancellation mechanisms does not result in a sum of their individual cancellations

# Characterization of Average Cancellation

- Digital cancellation

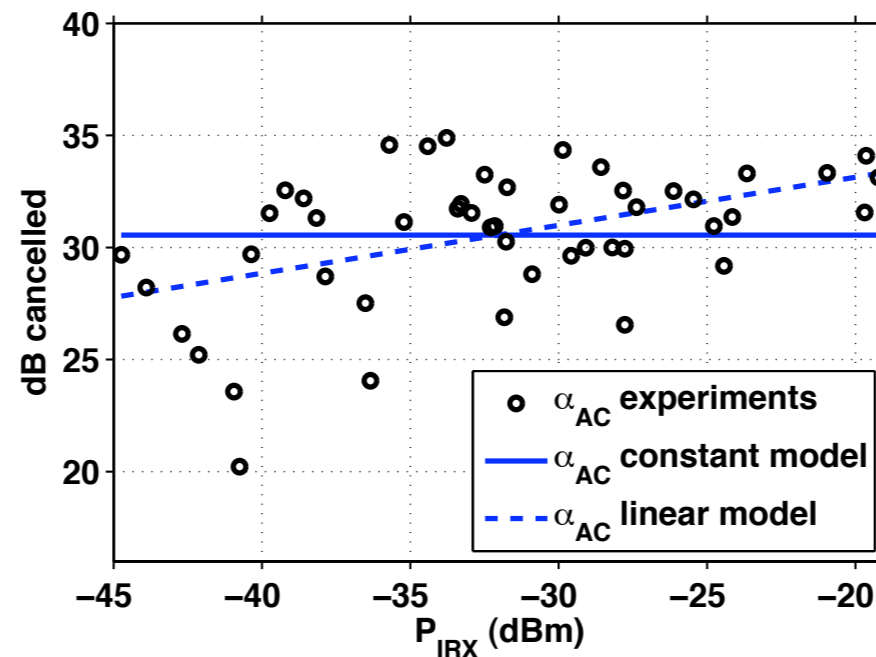
$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



Max cancellation : 27 dB

- Analog cancellation

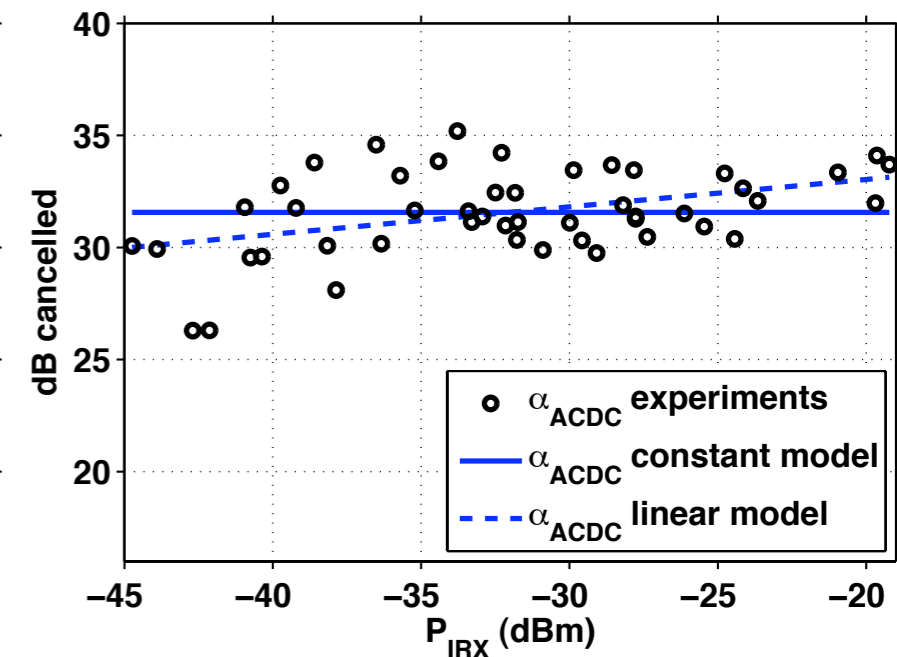
$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



Max cancellation : 35 dB

- Analog and digital cancellation

$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



Max cancellation : 36 dB

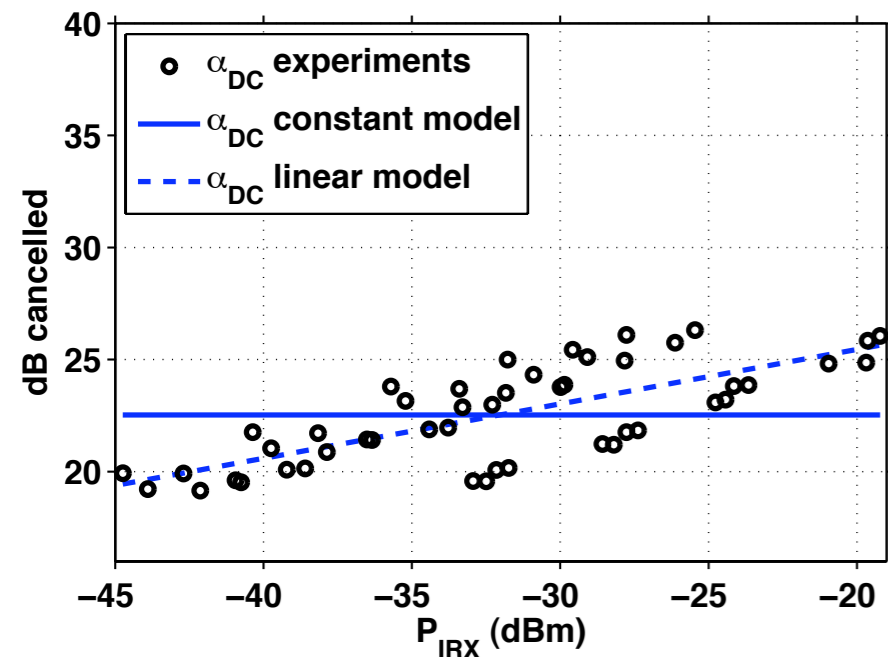
- Result 2:

(a) Concatenation of cancellation mechanisms does not result in a sum of their individual cancellations

# Characterization of Average Cancellation

- Digital cancellation

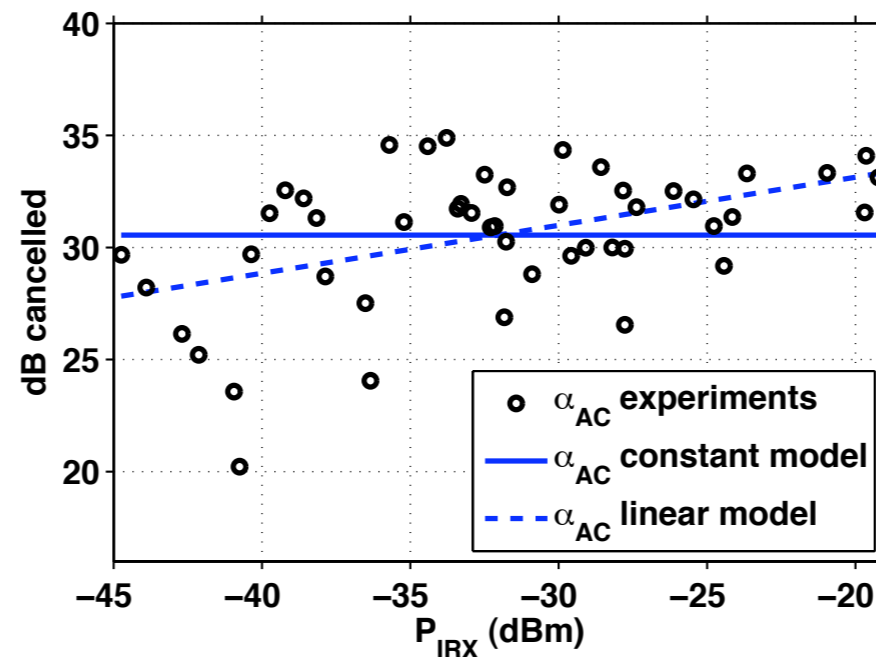
$$\alpha_{DC} = P_{IRX} - P_{IDC}$$



Max cancellation : 27 dB

- Analog cancellation

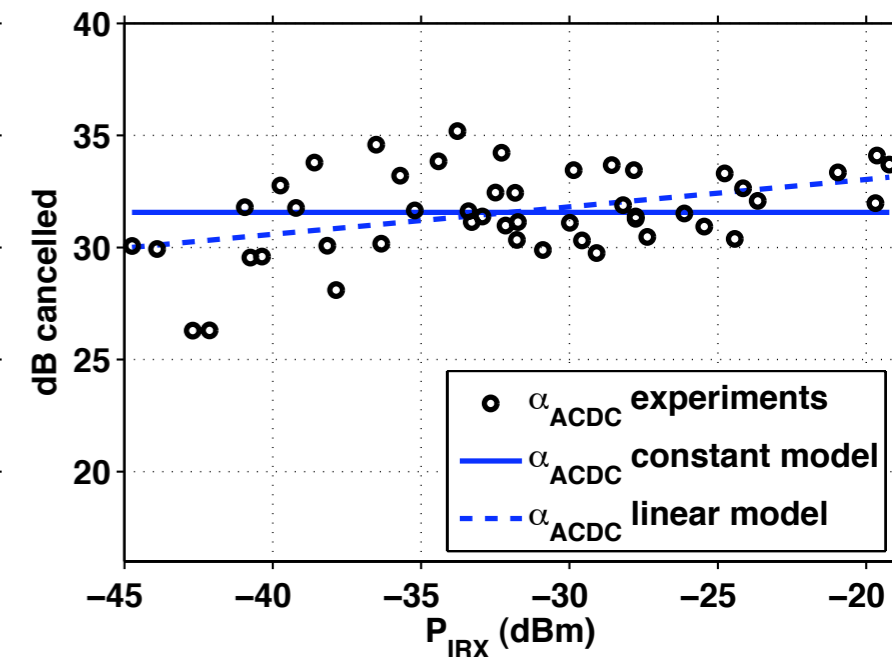
$$\alpha_{AC} = P_{IRX} - P_{IAC}$$



Max cancellation : 35 dB

- Analog and digital cancellation

$$\alpha_{ACDC} = P_{IRX} - P_{IACDC}$$



Max cancellation : 36 dB

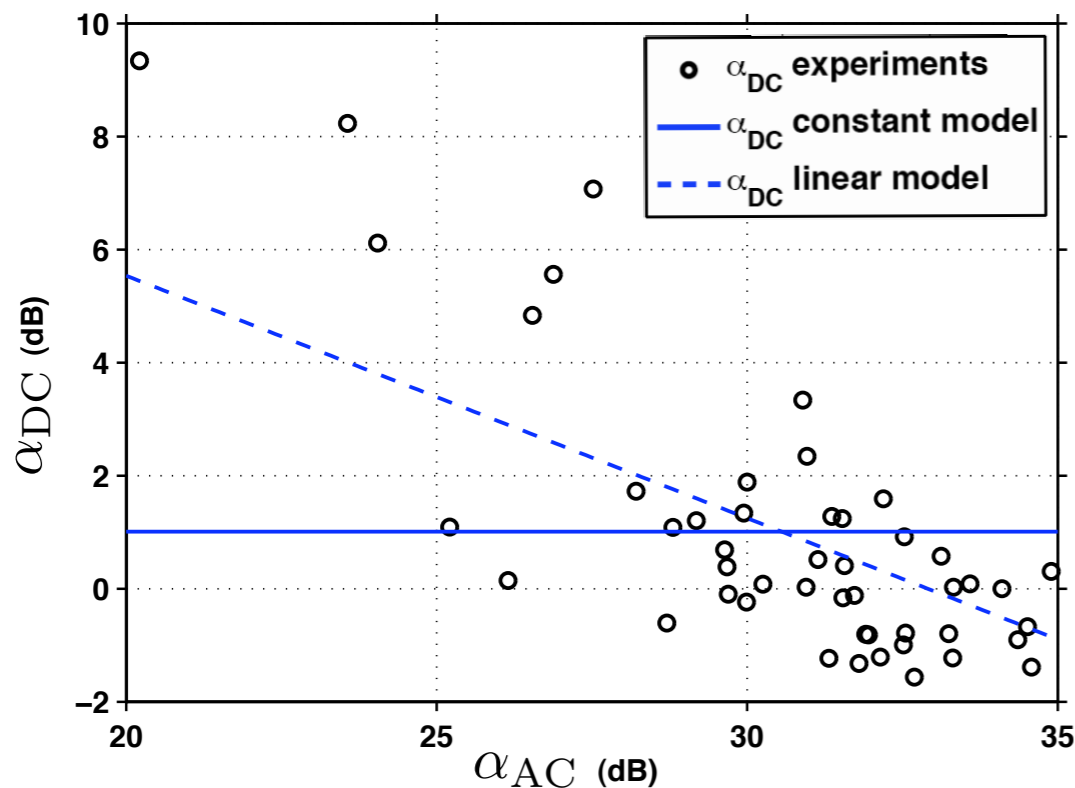
- Result 2:

- Concatenation of cancellation mechanisms does not result in a sum of their individual cancellations
- As the performance of analog cancellation gets better, the effectiveness of digital cancellation after analog cancellation reduces (observed on average and per frame)

# Characterization of Average Cancellation

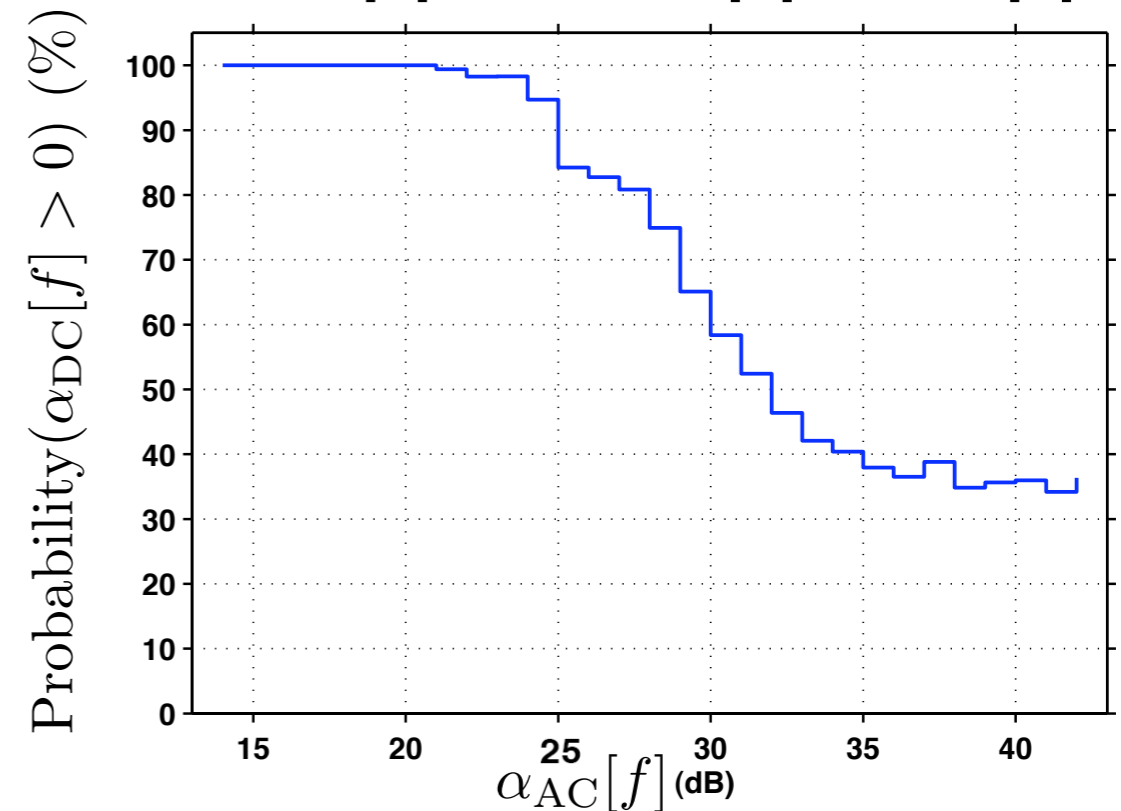
- Average performance

$$\alpha_{DC} = \alpha_{ACDC} - \alpha_{AC}$$



- Per frame performance

$$\alpha_{DC}[f] = \alpha_{ACDC}[f] - \alpha_{AC}[f]$$



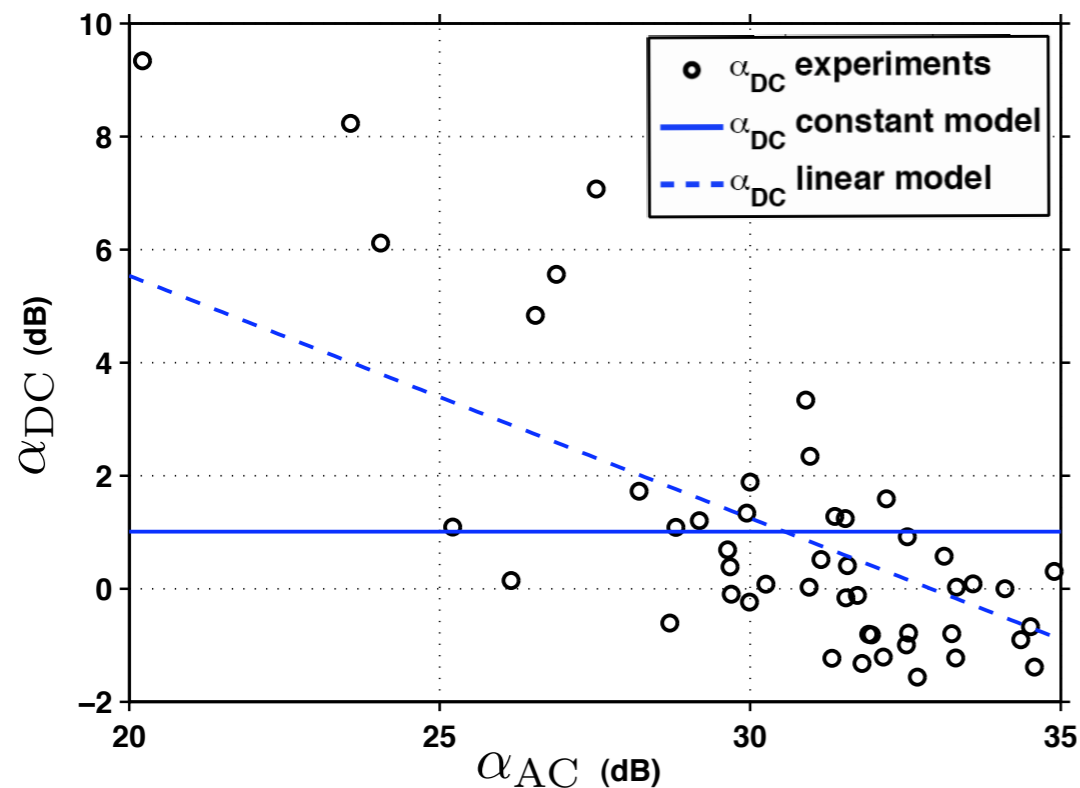
- Result 2:

- (a) Concatenation of cancellation mechanisms does not result in a sum of their individual cancellations
- (b) As the performance of analog cancellation gets better, the effectiveness of digital cancellation after analog cancellation reduces (observed on average and per frame)

# Characterization of Average Cancellation

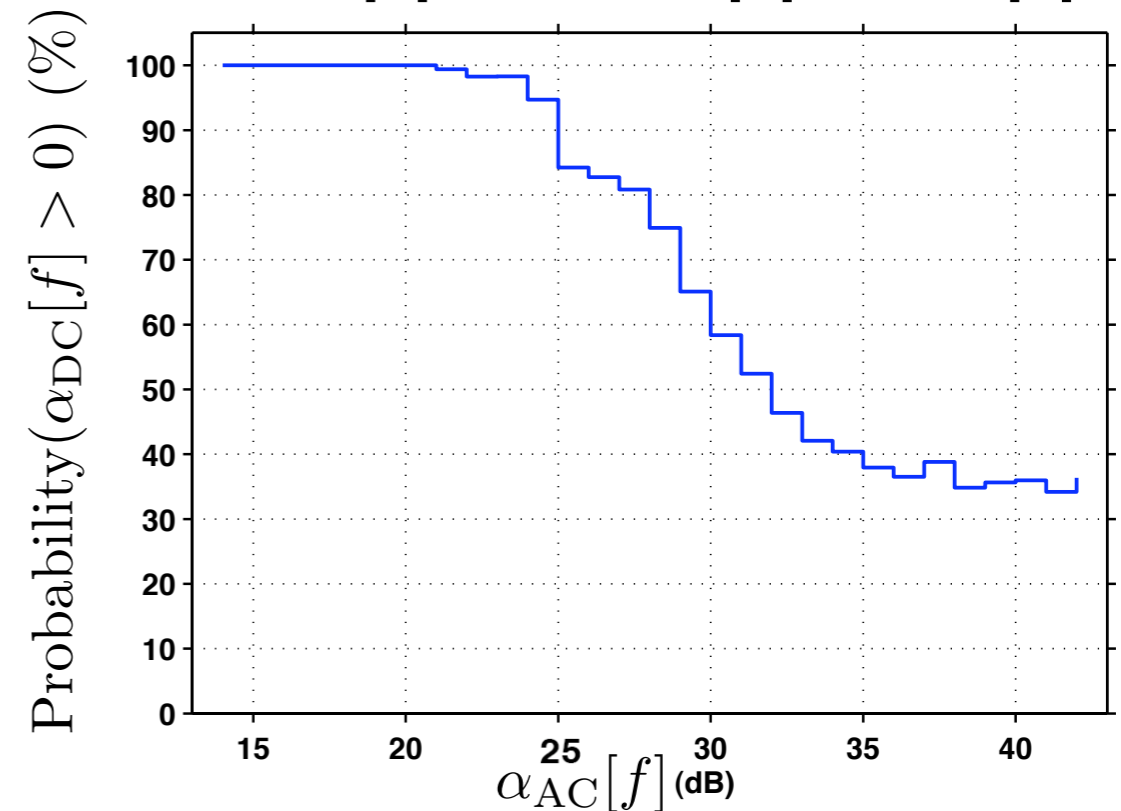
- Average performance

$$\alpha_{DC} = \alpha_{ACDC} - \alpha_{AC}$$



- Per frame performance

$$\alpha_{DC}[f] = \alpha_{ACDC}[f] - \alpha_{AC}[f]$$



- Reasons for Result 2:

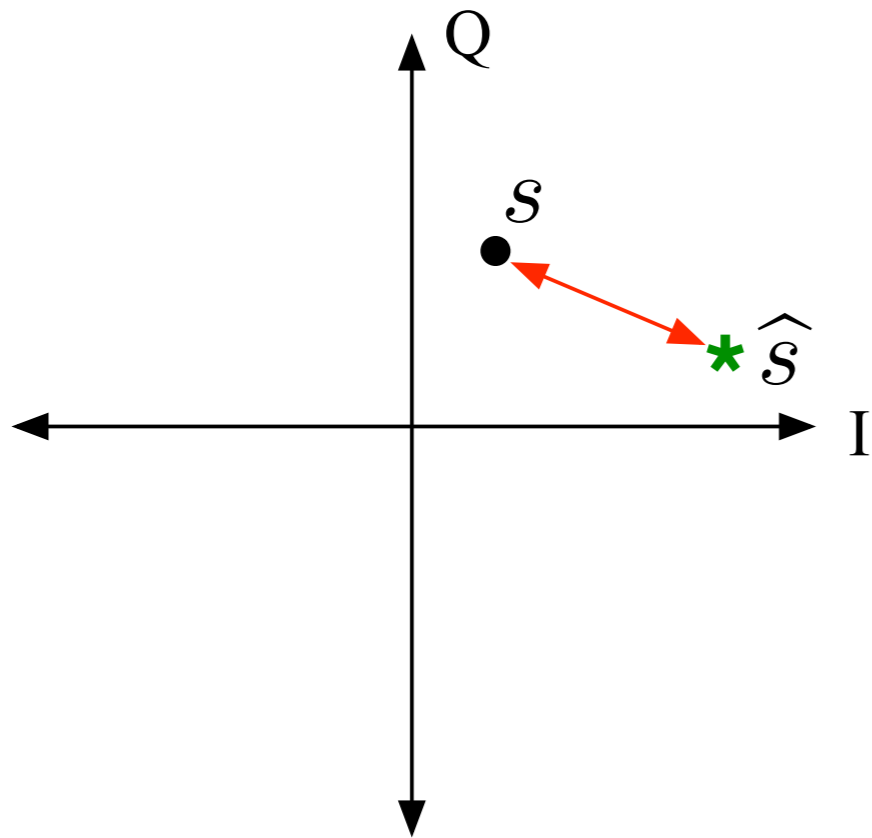
- As residual interference becomes smaller the effectiveness of cancelling the residual reduces
- If analog cancellation could achieve  $\infty$  dB of cancellation then digital cancellation would be unnecessary
- Furthermore applying digital cancellation would increase the noise

# Summary of Results

- Characterization of self-interference cancellation mechanisms
  - Amount of cancellation
  - Impact on full-duplex achievable rate performance
  
- Comparison with half-duplex systems
  - Demonstrated that full-duplex can achieve higher rates than half-duplex
  
- Duarte et al. *Full-Duplex Wireless Communications using Off-The-Shelf Radios: Feasibility and First Results*. Asilomar 2010.
- Duarte et al. *Experiment-Driven Characterization of Full-duplex Wireless Systems*. Submitted to IEEE Trans. Wireless 2011.

# Computation of Achievable Sum Rate

- Achievable Sum Rate (ASR) b/s/Hz computed based on post processing SINR



- Compute SINR per frame

$$\text{SINR}[f] = \frac{E[|s|^2]}{E[|s - \hat{s}|^2]}$$

- Compute achievable rate

$$\text{AR} = E[\log(1 + \text{SINR}[f])]$$

- Sum rate full-duplex

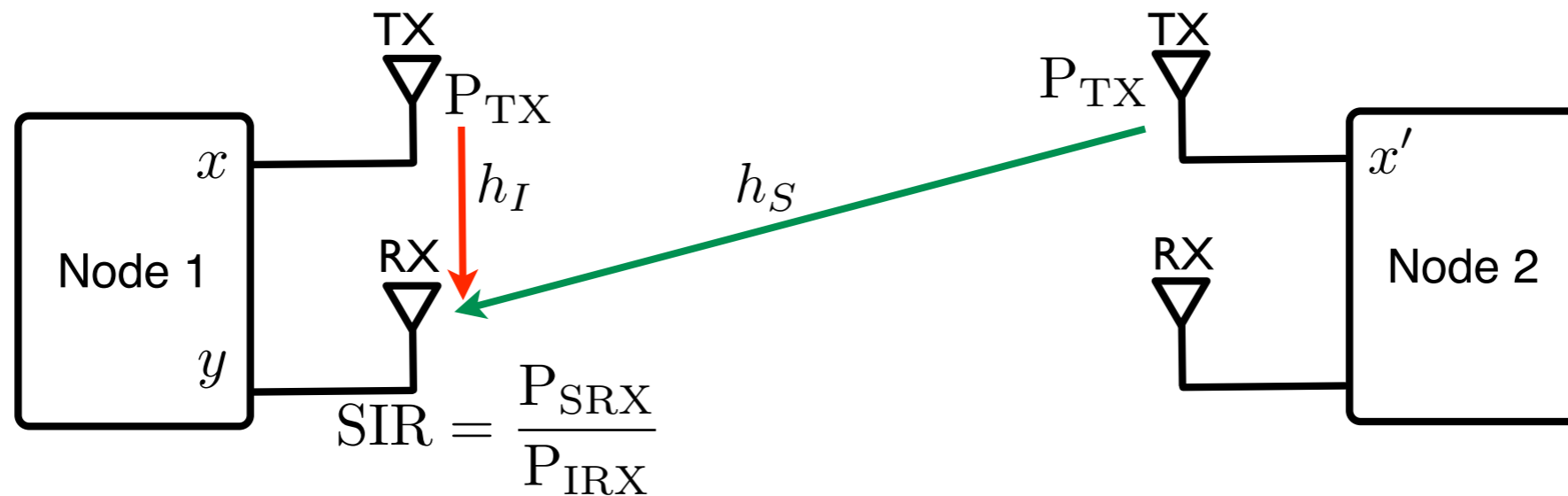
$$\text{ASR} = \text{AR}_{12} + \text{AR}_{21}$$

- Sum rate half-duplex

$$\text{ASR} = \frac{1}{2}\text{AR}_{12} + \frac{1}{2}\text{AR}_{21}$$

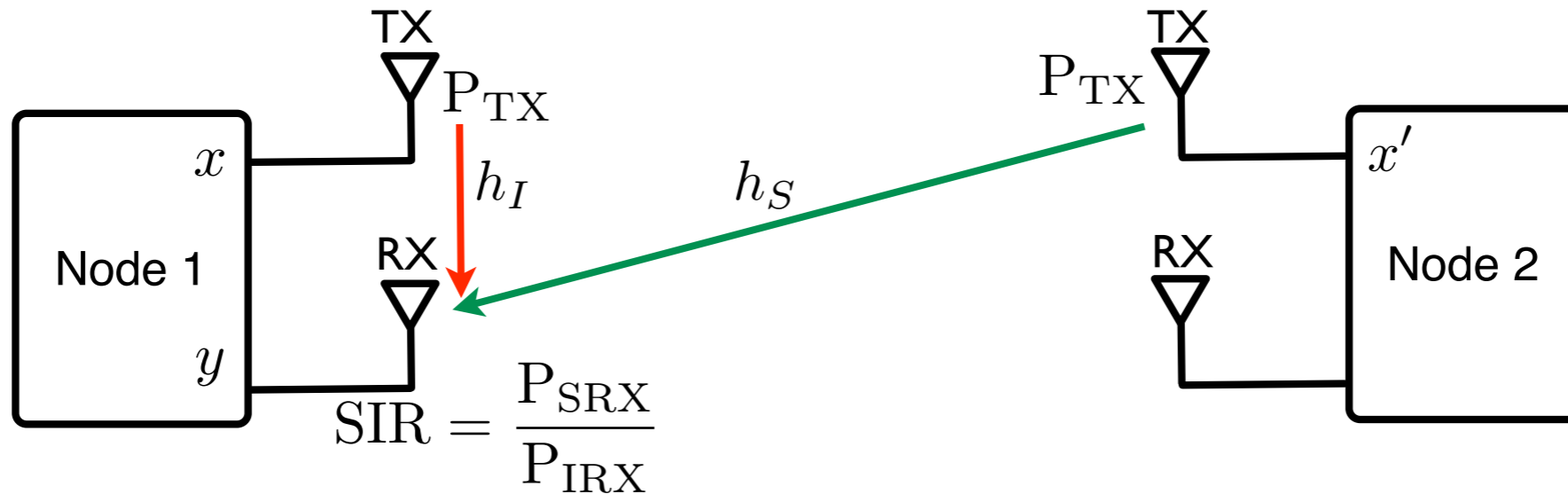


# Achievable Sum Rate Analysis



- Result 3:
  - For a fixed SIR at Rx antenna, increasing the transmit power increases the total achievable rate.
- Reasons for Result 3 ...

# Achievable Sum Rate Analysis



- Without active cancellation

$$y = h_S x' + h_I x + z$$

- With active cancellation

$$y = h_S x' + (h_I - \hat{h}_I) x + z$$

- With active cancellation rewrite as

$$y = h_S x' + h_R \sqrt{\frac{\Omega}{\alpha}} x + z \longrightarrow \text{SINR} = \frac{1}{\frac{1}{\alpha \text{SIR}} + \frac{1}{\text{SNR}}}$$

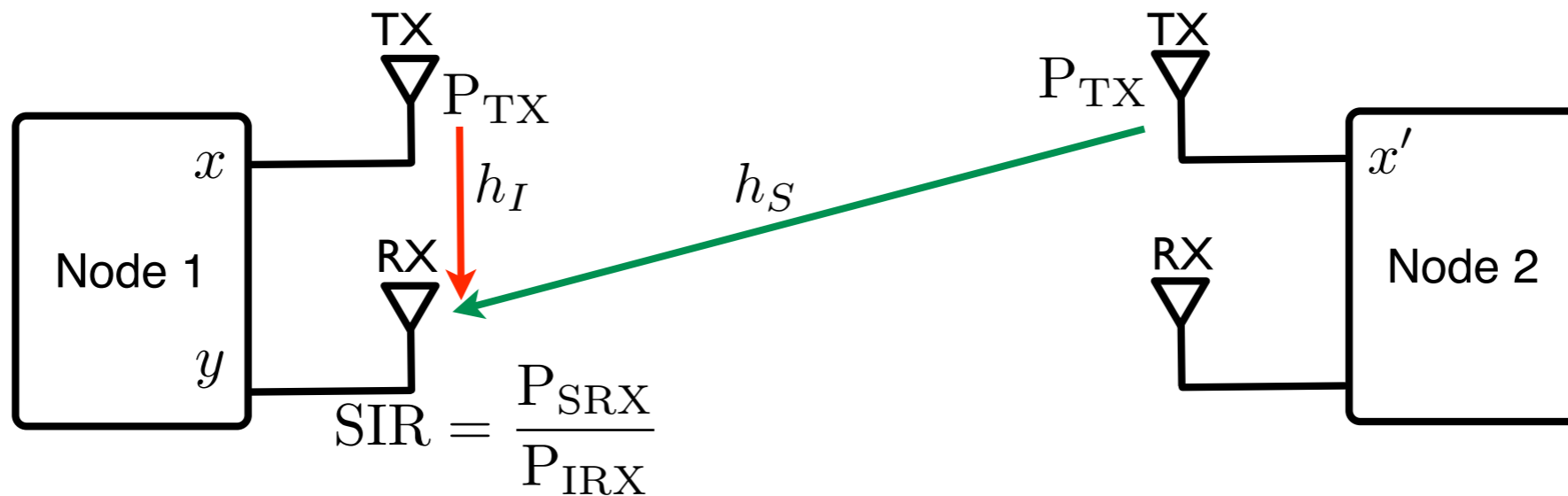
$h_R$  : normalized residual channel

$\Omega$  : due to antenna separation

$\alpha$  : due to active cancellation

- Duarte et al. *Experiment-Driven Characterization of Full-duplex Wireless Systems*. Submitted to IEEE Trans. Wireless 2011.

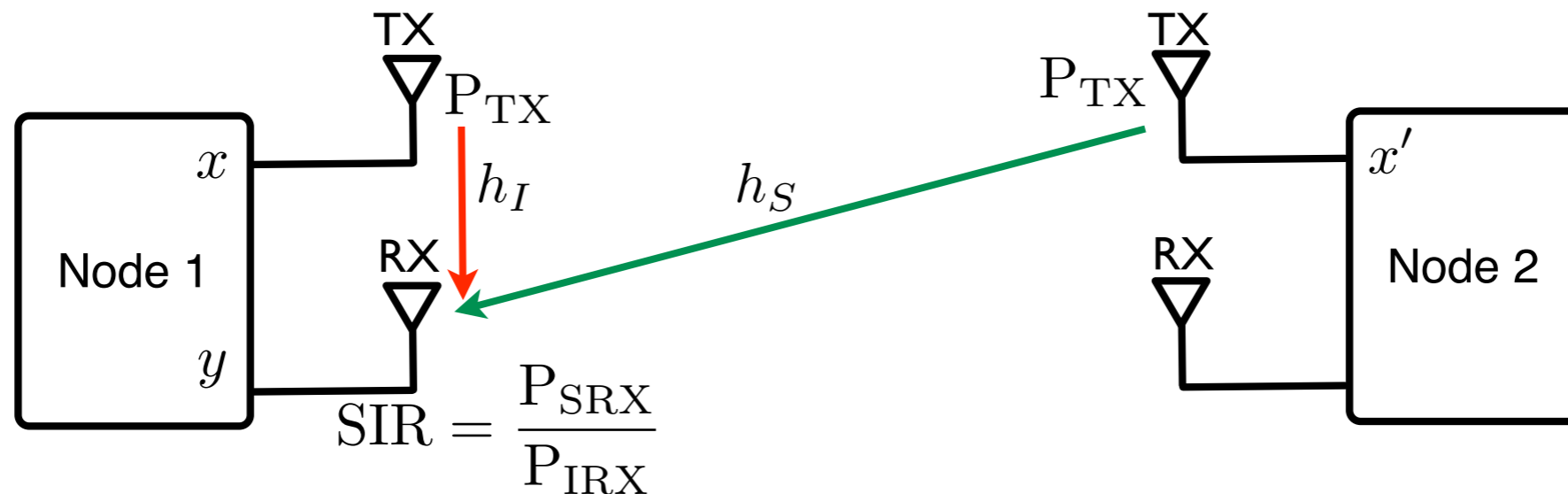
# Achievable Sum Rate Analysis



- Achievable sum rate

$$ASR = \log(1 + SINR_1) + \log(1 + SINR_2) \quad SINR_i = \frac{1}{\frac{1}{\alpha_i SIR_i} + \frac{1}{SNR_i}}$$

# Achievable Sum Rate Analysis



- Achievable sum rate

$$ASR = \log(1 + SINR_1) + \log(1 + SINR_2) \quad SINR_i = \frac{1}{\frac{1}{\alpha_i SIR_i} + \frac{1}{SNR_i}}$$

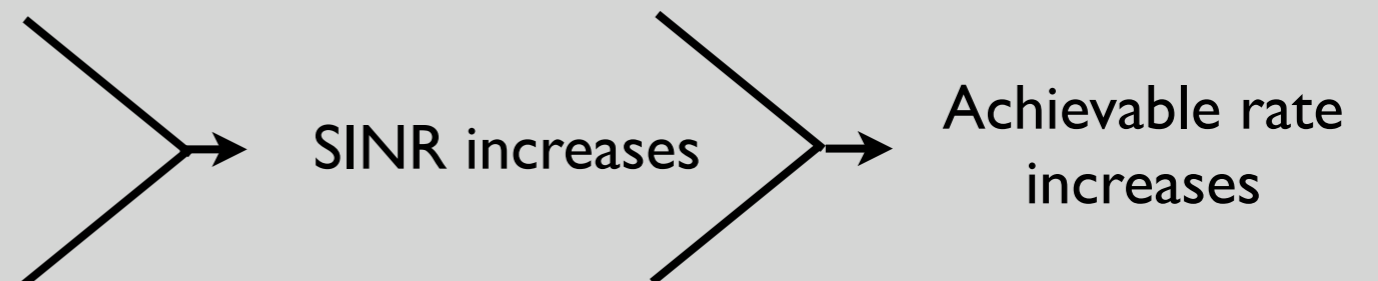
- Result 3:

- For a fixed SIR at Rx antenna, increasing the transmit power increases the total achievable rate.

- Reasons for Result 3:

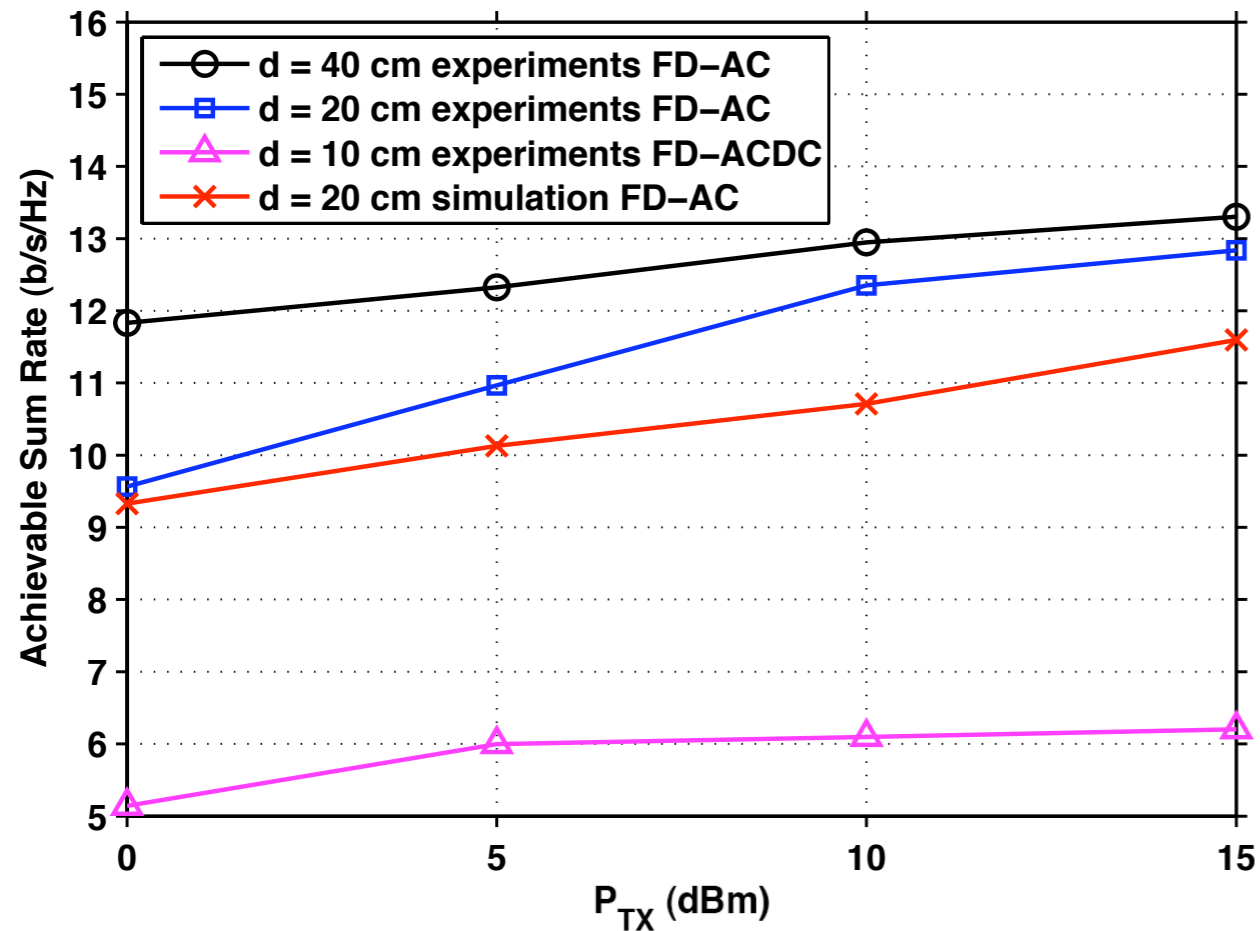
- If  $P_{TX}$  at both nodes increases by same amount then

- SIR doesn't change
- $\alpha$  increases (from Result 1)
- SNR increases



# Achievable Sum Rate Analysis

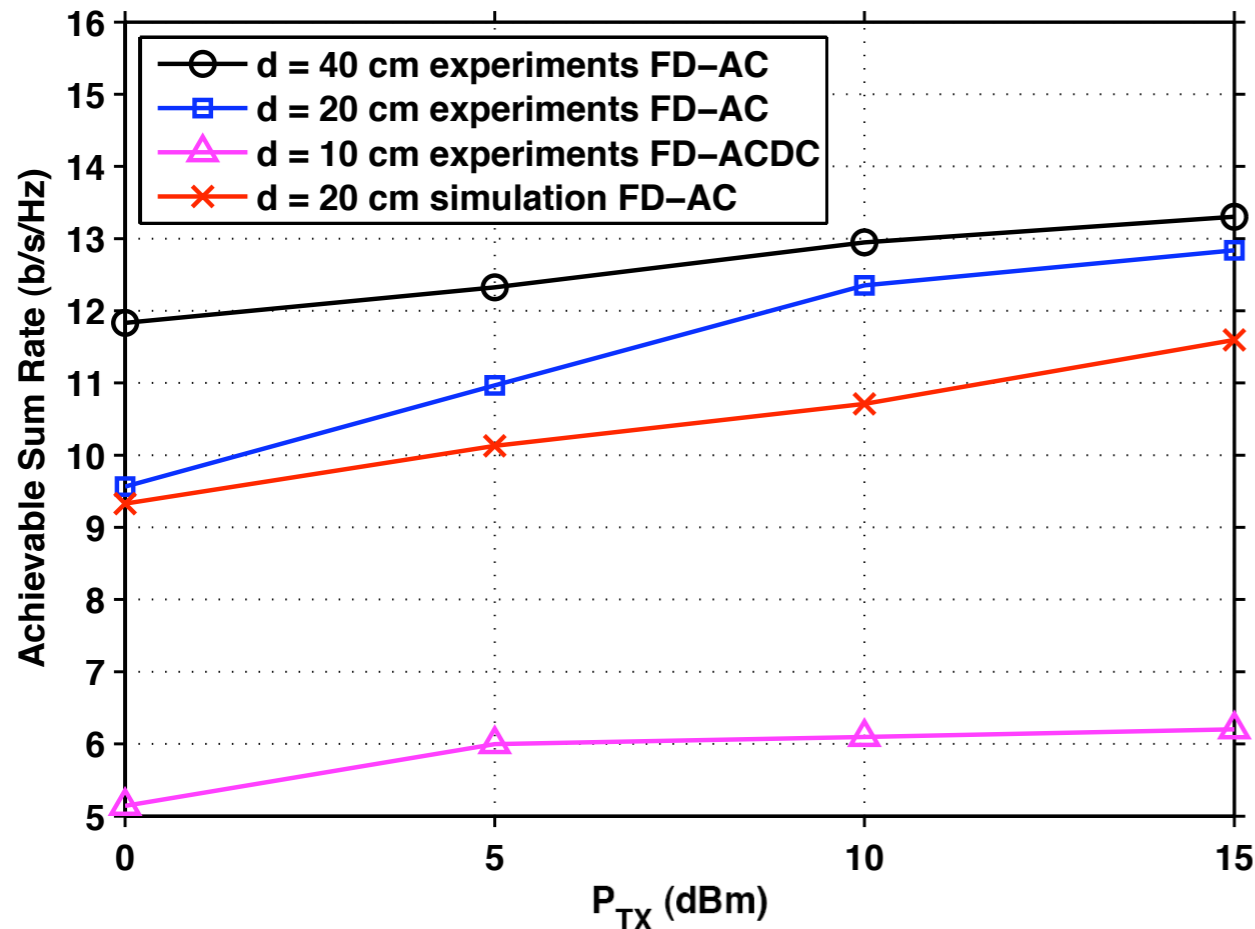
- Result 3 demonstrated in experiments and simulation



- FD-AC: Full-duplex with antenna separation and Analog Cancellation
- FD-ACDC: Full-duplex with antenna separation and combined Analog and Digital Cancellation

# Achievable Sum Rate Analysis

- Result 3 demonstrated in experiments and simulation



- FD-AC: Full-duplex with antenna separation and Analog Cancellation
- FD-ACDC: Full-duplex with antenna separation and combined Analog and Digital Cancellation

- Simulation results obtained using model

$$y = h_S x' + h_R \sqrt{\frac{\Omega}{\alpha}} x + z$$

$$\text{SINR} = \frac{1}{\frac{1}{\alpha \text{SIR}} + \frac{1}{\text{SNR}}}$$

- Setting

$$\text{SNR} = \infty$$

$$\text{SIR} = \text{Measured in experiments}$$

$$\alpha = \text{Linear fit}$$

- Linear fit model seems reasonably accurate

# Achievable Sum Rate Analysis

- Result 4:
  - Best performance is achieved when applying digital cancellation selectively based on measured suppression values
- Reasons for Result 4:
  - For each frame decide if digital cancellation after analog cancellation should be applied or not as follows
    - Use training at the beginning of the frame to estimate  $\alpha_{AC}[f]$  and  $\alpha_{ACDC}[f]$
    - Apply digital cancellation after analog cancellation during frame  $f$  only if

$$\alpha_{ACDC}[f] - \alpha_{AC}[f] > 0$$

# Achievable Sum Rate Analysis

- Result 4:
  - Best performance is achieved when applying digital cancellation selectively based on measured suppression values
- Reasons for Result 4:
  - Follows from Result 2:
    - (a) Concatenation of cancellation mechanisms does not result in a sum of their individual cancellations
    - (b) As the performance of analog cancellation gets better, the effectiveness of digital cancellation after analog cancellation reduces (observed on average and per frame)
- For each frame decide if digital cancellation after analog cancellation should be applied or not as follows
  - Use training at the beginning of the frame to estimate  $\alpha_{AC}[f]$  and  $\alpha_{ACDC}[f]$
  - Apply digital cancellation after analog cancellation during frame  $f$  only if

$$\alpha_{ACDC}[f] - \alpha_{AC}[f] > 0$$

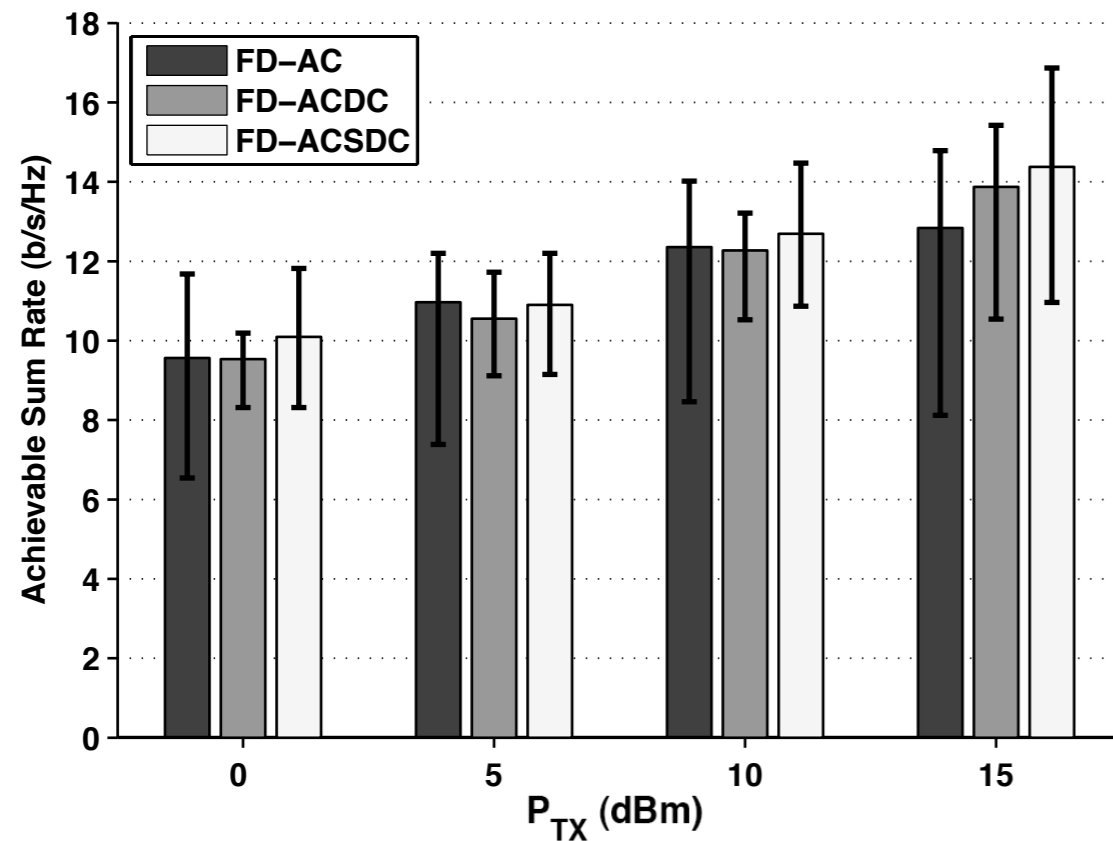


# Achievable Sum Rate Analysis

- Result 4:

- Best performance is achieved when applying digital cancellation selectively based on measured suppression values

- Experiment results

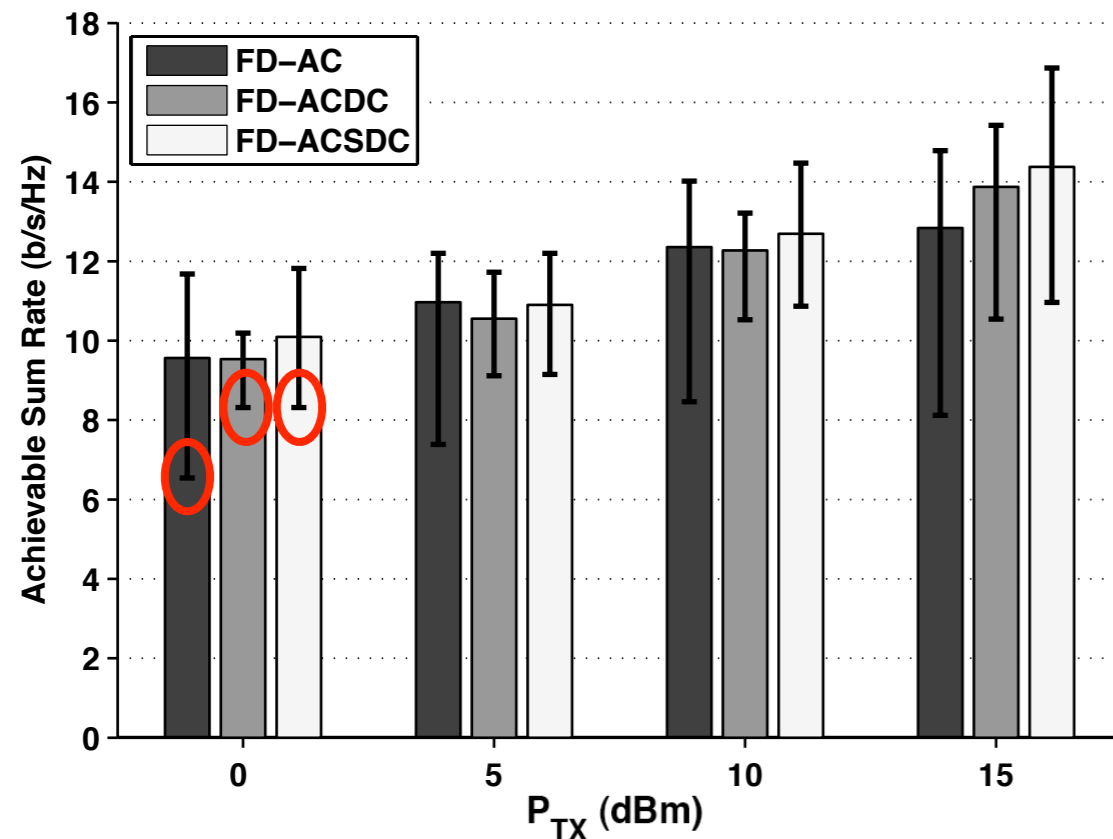


- FD-AC: Full-duplex with antenna separation and Analog Cancellation
- FD-ACDC: Full-duplex with antenna separation and combined Analog and Digital Cancellation
- FD-ACSDC: Full-duplex with antenna separation and combined Analog and Selective Digital Cancellation

# Achievable Sum Rate Analysis

- Result 4:
  - Best performance is achieved when applying digital cancellation selectively based on measured suppression values

- Experiment results



- FD-AC: Full-duplex with antenna separation and Analog Cancellation
- FD-ACDC: Full-duplex with antenna separation and combined Analog and Digital Cancellation
- FD-ACSDC: Full-duplex with antenna separation and combined Analog and Selective Digital Cancellation

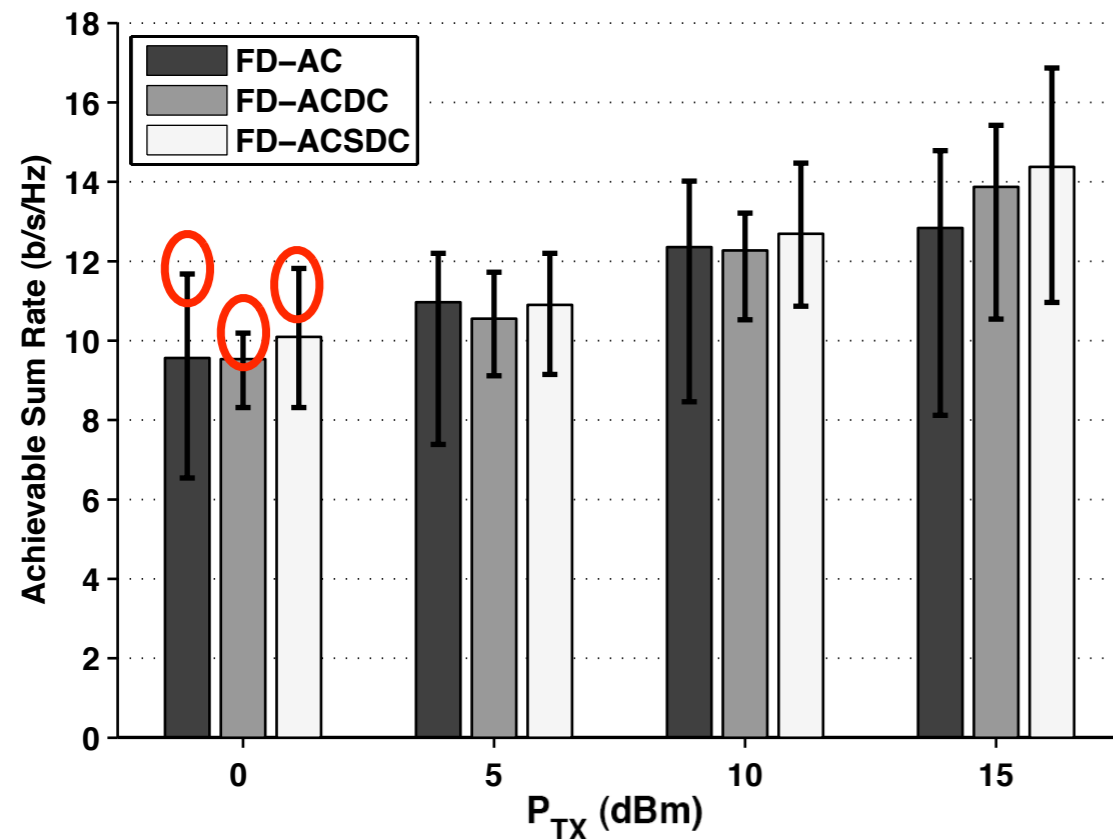
- Benefits of selective digital cancellation

- Uses digital cancellation as a safety net in frames where analog cancellation delivers poor performance
- Avoids adding noise to the system when analog cancellation delivers good performance
- Results in largest average achievable sum rate

# Achievable Sum Rate Analysis

- Result 4:
  - Best performance is achieved when applying digital cancellation selectively based on measured suppression values

- Experiment results



- FD-AC: Full-duplex with antenna separation and Analog Cancellation
- FD-ACDC: Full-duplex with antenna separation and combined Analog and Digital Cancellation
- FD-ACSDC: Full-duplex with antenna separation and combined Analog and Selective Digital Cancellation

- Benefits of selective digital cancellation

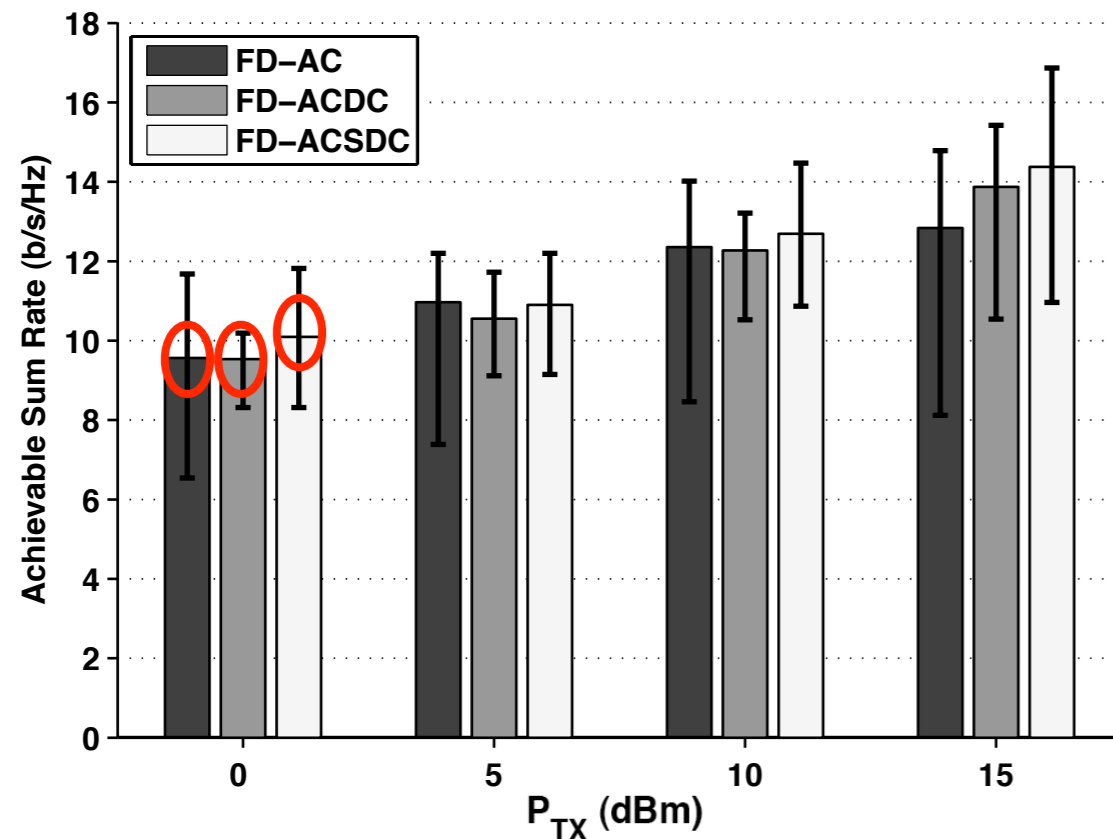
- Uses digital cancellation as a safety net in frames where analog cancellation delivers poor performance
- Avoids adding noise to the system when analog cancellation delivers good performance
- Results in largest average achievable sum rate

# Achievable Sum Rate Analysis

- Result 4:

- Best performance is achieved when applying digital cancellation selectively based on measured suppression values

- Experiment results



- FD-AC: Full-duplex with antenna separation and Analog Cancellation
- FD-ACDC: Full-duplex with antenna separation and combined Analog and Digital Cancellation
- FD-ACSDC: Full-duplex with antenna separation and combined Analog and Selective Digital Cancellation

- Benefits of selective digital cancellation

- Uses digital cancellation as a safety net in frames where analog cancellation delivers poor performance
- Avoids adding noise to the system when analog cancellation delivers good performance
- Results in largest average achievable sum rate

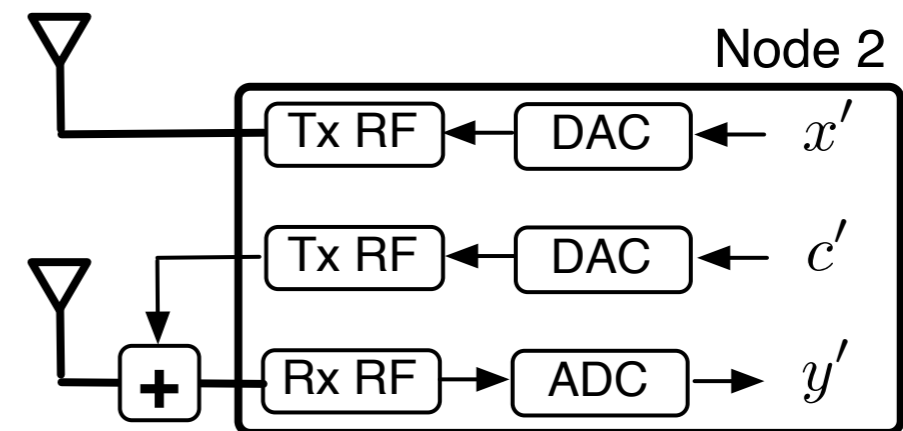
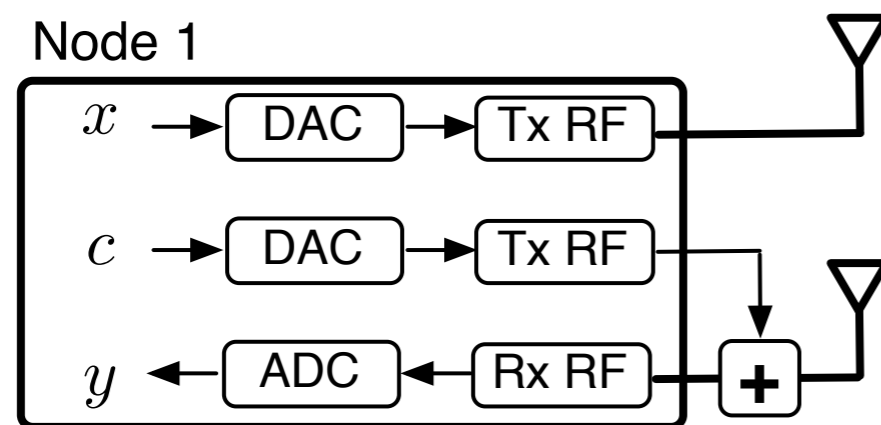
# Summary of Results

- Characterization of self-interference cancellation mechanisms
  - Amount of cancellation
  - Impact on full-duplex achievable rate performance
  
- Comparison with half-duplex systems
  - Demonstrated that full-duplex can achieve higher rates than half-duplex
  
- Duarte et al. *Full-Duplex Wireless Communications using Off-The-Shelf Radios: Feasibility and First Results*. Asilomar 2010.
- Duarte et al. *Experiment-Driven Characterization of Full-duplex Wireless Systems*. Submitted to IEEE Trans. Wireless 2011.

# Full-Duplex vs. Half-Duplex

Compare half-duplex and full-duplex systems that use same resources

	Full-duplex with analog cancellation	Half-duplex 2x1 Alamouti
Antennas per node	2	2
Tx RF radios per node	2	2
Rx RF radios per node	1	1
Tx power per antenna	$P_{TX}$	$P_{TX}$

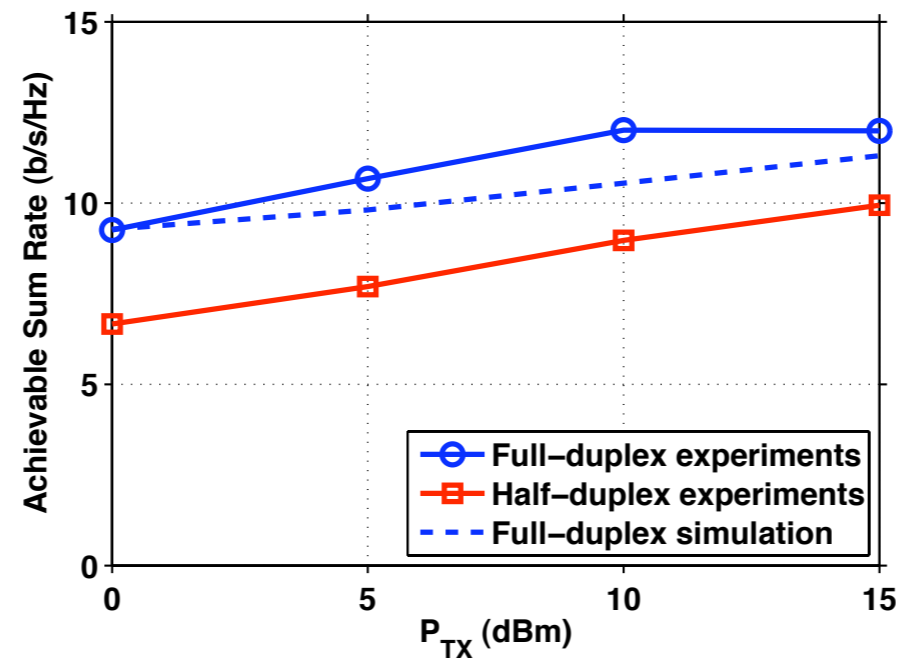


# Full-Duplex vs. Half-Duplex

●  $d = 10$  cm

●  $d = 20$  cm

●  $d = 40$  cm

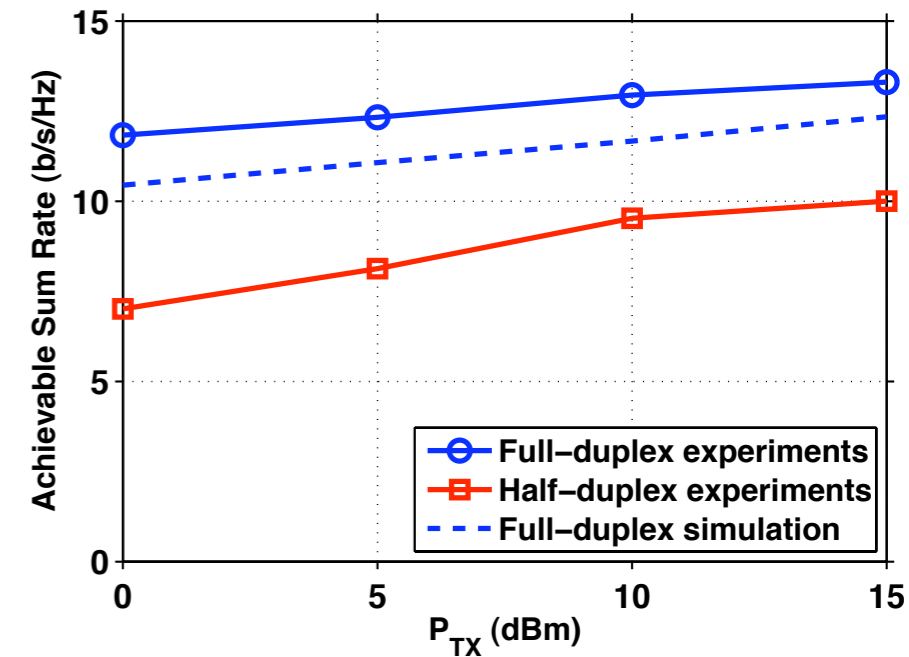
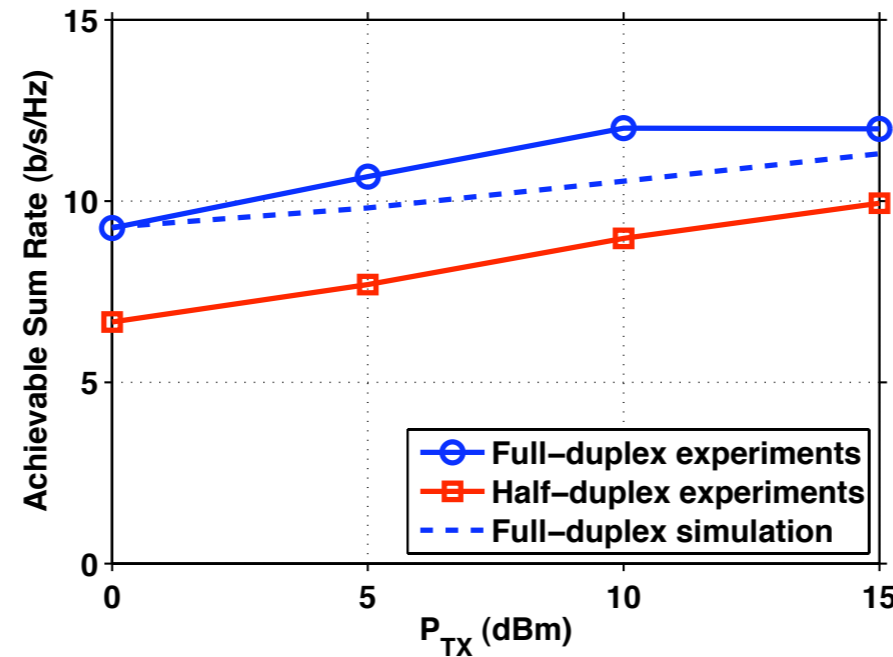


# Full-Duplex vs. Half-Duplex

•  $d = 10$  cm

•  $d = 20$  cm

•  $d = 40$  cm

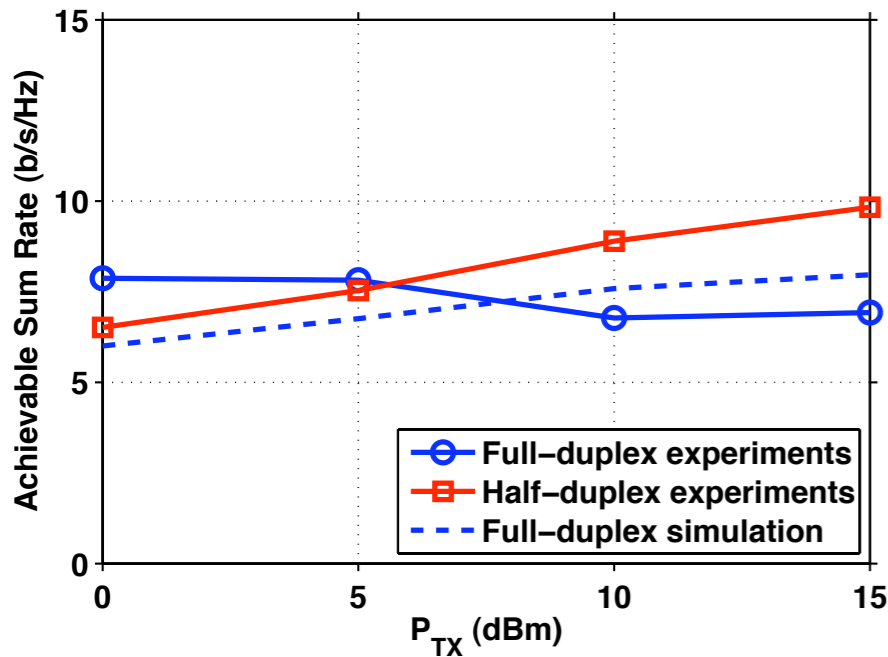


- Full-duplex can achieve higher rates than half-duplex
- The linear fit model is reasonable accurate

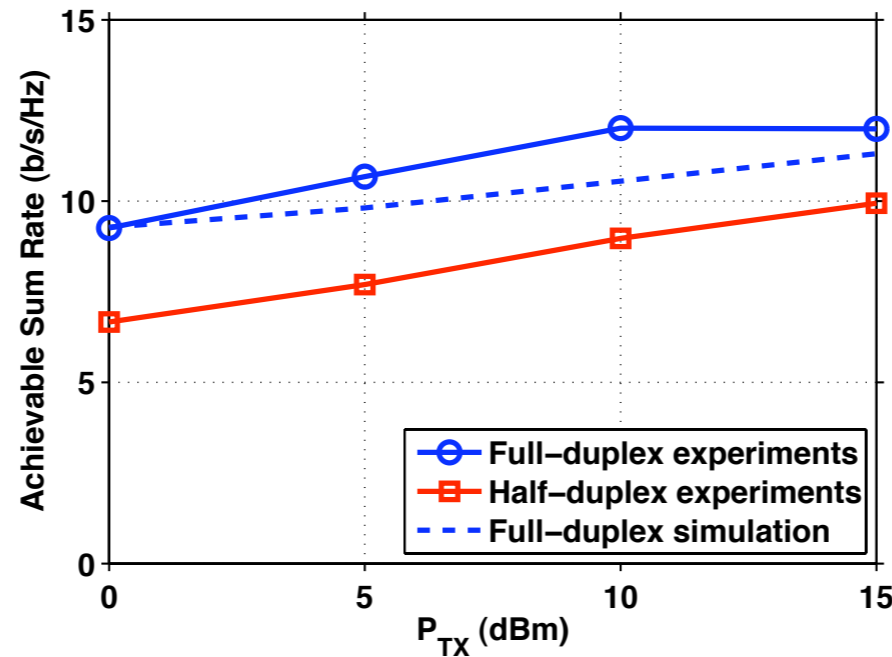


# Full-Duplex vs. Half-Duplex

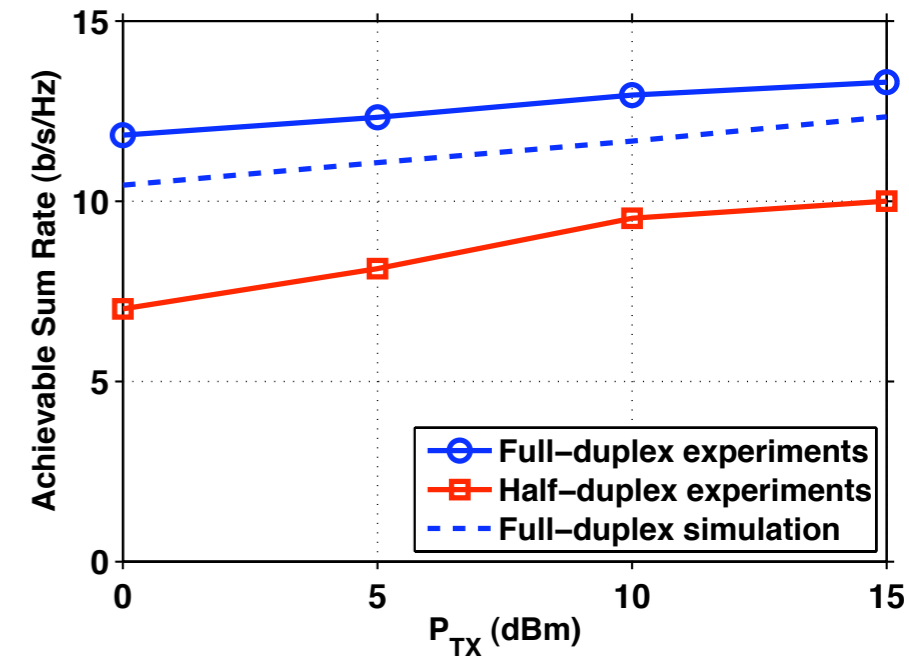
●  $d = 10$  cm



●  $d = 20$  cm



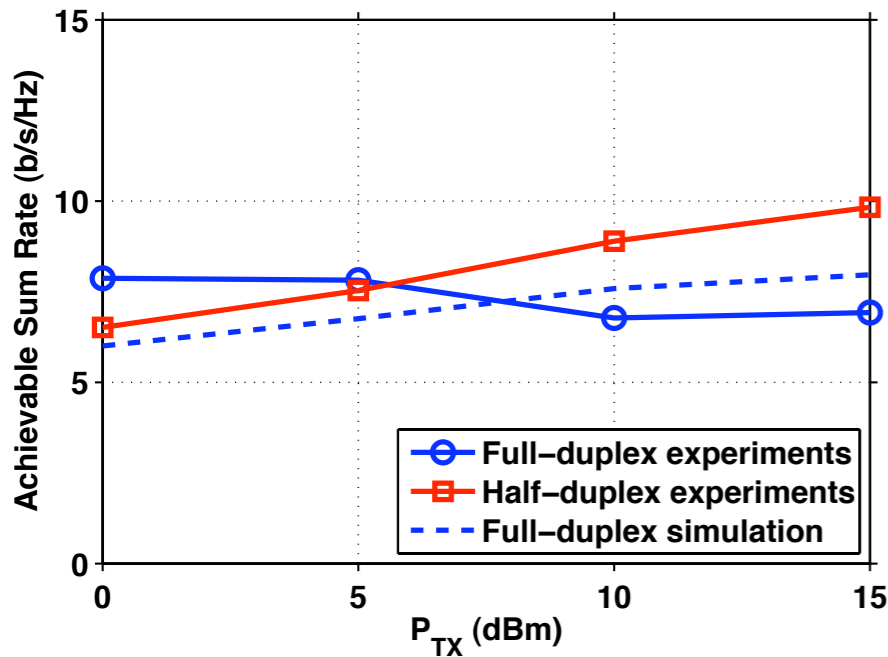
●  $d = 40$  cm



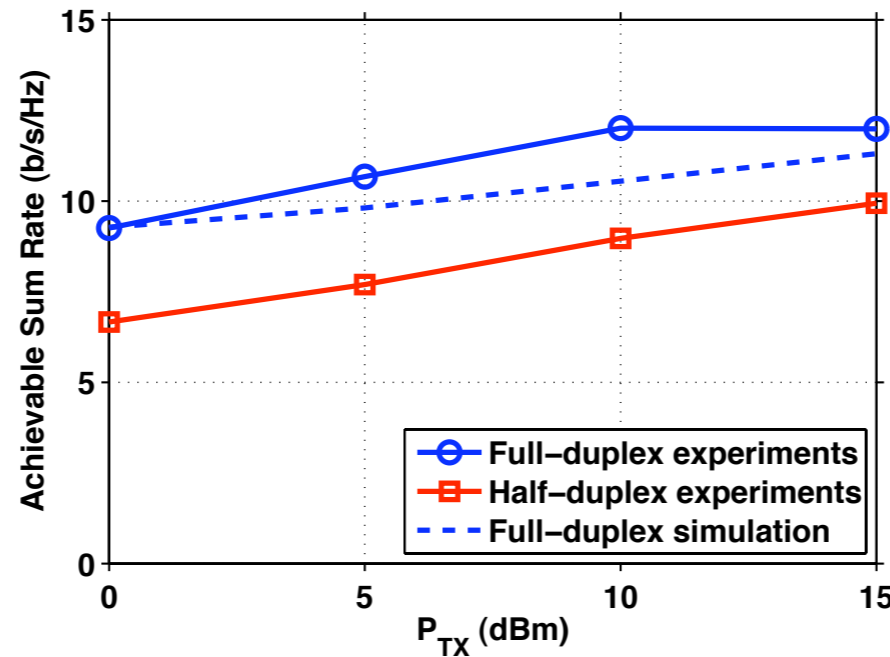
- Full-duplex can achieve higher rates than half-duplex
- The linear fit model is reasonable accurate
- Close antennas imply in some scenarios half-duplex wins-out

# Full-Duplex vs. Half-Duplex

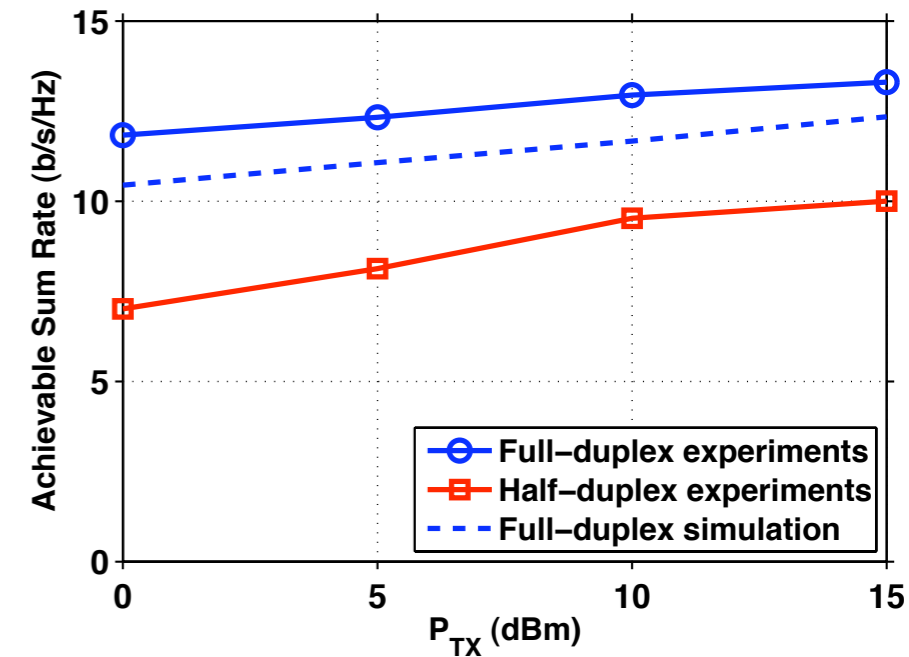
●  $d = 10$  cm



●  $d = 20$  cm



●  $d = 40$  cm



- Full-duplex can achieve higher rates than half-duplex
- The linear fit model is reasonable accurate
- Close antennas imply in some scenarios half-duplex win-out
- Full-duplex without analog cancellation and only digital cancellation always performs worse than half-duplex due to quantization noise
  - Duarte et al. *Full-Duplex Wireless Communications using Off-The-Shelf Radios: Feasibility and First Results*. Asilomar 2010.

# Conclusions

- Full-duplex can achieve higher rates than half-duplex.
- Amount of active cancellation increases as the received self-interference power increases.
- At a constant SIR@Rx antenna more interference is actually good. It allows better cancellation and thus improved rates.
- Digital cancellation is more effective when applied selectively after analog cancellation.

# Conclusions

- Full-duplex can achieve higher rates than half-duplex.
- Amount of active cancellation increases as the received self-interference power increases.
- At a constant SIR@Rx antenna more interference is actually good. It allows better cancellation and thus improved rates.
- Digital cancellation is more effective when applied selectively after analog cancellation.

## Recent and ongoing work at Rice

- Asynchronous full-duplex.
  - Receive-while-sending.
  - (not send-while-receiving)
- Antenna design and MAC protocols.
- MIMO and OFDM analysis.

Everett et. al. *Empowering Full-Duplex Wireless Communication by Exploiting Directional Diversity*. Asilomar 2011.

Sahai et al. *Pushing the Limits of Full-Duplex: Design and Real-Time Implementation*. Tech. Report 2011. Rice University.